Programming in Python[1]

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Lecture XVI: A game of life

A game of life

In 1970, J.H. Conway proposed his Game of Life, a simulation on a 2D grid:

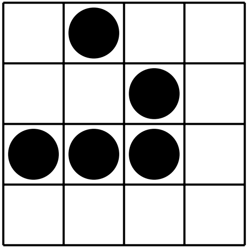
1. Every cell can be *alive* or *dead*: the game start with a population of alive cells (*seed*)
2. any alive cell with less of 2 alive neighbours dies (*underpopulation*)
3. any alive cell with more than 3 alive neighbours dies (*overpopulation*)
4. any dead cell with exactly 3 alive neighbours becomes alive (*reproduction*)

The game is surprisingly rich: many mathematicians, computer scientists, biologists. . . spent their careers on the emerging patterns!

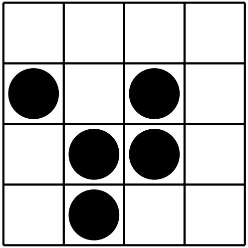
Life forms

There are names for many “life forms”: *still lifes*, *oscillators*, *starships*. . .

A famous starship is the glider:



1	1	2	1
3	5	3	2
1	3	2	2
2	3	2	1



The glider repeats itself in another position after 4 generations.

Python implementation

To implement a Game of Life simulation in Python, we can:

- use a `ndarray` for the grid
- each cell contains 0 (dead) or 1 (alive)
- for simplicity we can add a "border" of zeros

0	0	0	0	0
0	1	1	1	0
0	1	0	1	0
0	1	1	0	0
0	0	0	0	0

Avoiding loops

For a 1-D array `X`

0	**1**	**1**	**0**	**1**	0

All the neighbours on the right `X[2:]`

0	**1**	**1**	**0**	**1**	0

All the neighbours on the left `X[:-2]`

What does `X[2:] + X[:-2]` represent? The sum is (yellow) element by (yellow) element, the result is: `[1,1,2,0]`
Can you think to a similar solution for the 2-D case?

Avoiding loops

0	0	0	0	0	0
0	**0**	**1**	**0**	**0**	0
0	**0**	**0**	**1**	**0**	0
0	**1**	**1**	**1**	**0**	0
0	**0**	**0**	**0**	**0**	0
0	0	0	0	0	0

```
X[1:-1, 2:]
```

Avoiding loops

0	0	0	0	0	0
0	**0**	**1**	**0**	**0**	0
0	**0**	**0**	**1**	**0**	0
0	**1**	**1**	**1**	**0**	0
0	**0**	**0**	**0**	**0**	0
0	0	0	0	0	0

`X[2:,2:]`

Avoiding loops

0	0	0	0	0	0
0	**0**	**1**	**0**	**0**	0
0	**0**	**0**	**1**	**0**	0
0	**1**	**1**	**1**	**0**	0
0	**0**	**0**	**0**	**0**	0
0	0	0	0	0	0

`X[2:,1:-1]`

Avoiding loops

0	0	0	0	0	0
0	**0**	**1**	**0**	**0**	0
0	**0**	**0**	**1**	**0**	0
0	**1**	**1**	**1**	**0**	0
0	**0**	**0**	**0**	**0**	0
0	0	0	0	0	0

`X[2:,1:-1]`

And other 5 matrices. . .

Avoiding loops

X

0	0	0	0	0	0
0	**0**	**1**	**0**	**0**	0
0	**0**	**0**	**1**	**0**	0
0	**1**	**1**	**1**	**0**	0
0	**0**	**0**	**0**	**0**	0
0	0	0	0	0	0

N

0	0	0	0	0	0
0	1	1	2	1	0
0	3	5	3	2	0
0	1	3	2	2	0
0	2	3	2	1	0
0	0	0	0	0	0

`X == 1` `N > 3`

Death by overpopulation: `X[(X == 1) & (N > 3)] = 0` (empty in this case!)