



PyQB

Monga

Monte Carlo  
approaches

Simulations

# Programming in Python<sup>1</sup>

Mattia Monga

Dip. di Informatica  
Università degli Studi di Milano, Italia

[mattia.monga@unimi.it](mailto:mattia.monga@unimi.it)

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# Lecture XI: Random numbers

# Status of the homework



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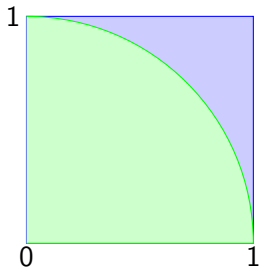
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|                      | accepted | done | ok |
|----------------------|----------|------|----|
| One triangle         | 22       | 13   | 11 |
| Triangle kinds       | 18       | 18   | 7  |
| Count chars          | 16       | 16   | 8  |
| Newton square root   | 14       | 14   | 6  |
| Pythagorean triplets | 18       | 10   | 10 |
| Sonar                | 16       | 16   | 6  |
| DNA Hamming          | 16       | 16   | 7  |
| DNA files            | 11       | 11   | 3  |
| Pseudo Random        | 6        | 6    | 1  |

# Example



- Blue square: 1
- Green area:  $\frac{\pi}{4}$

The **Monte Carlo** method consists of choosing sample experiments at random from a large set and then making deductions on the basis of the probabilities estimated from frequency of occurrences.

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# Example



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```
from random import random

def approx_pi(tries: int) -> float:
    """Return an approximation for pi.

    >>> from math import pi
    >>> from random import seed
    >>> seed(7897) # Tests should be reproducible
    >>> abs(4*approx_pi(1000) - pi) < 10e-2
    True

    >>> abs(4*approx_pi(100000) - pi) < abs(approx_pi(1000) - pi)
    True
    """

    assert tries > 0
    within_circle = 0
    for i in range(0, tries):
        x = random() # range [0,1)
        y = random()
        if x**2 + y**2 < 1:
            within_circle += 1
    return within_circle / tries
```



# Example

It's easy to extend to make this work for any function on  $[0, 1)$ .

```
from random import random
from collections.abc import Callable

def approx_fun(predicate: Callable[[float, float], bool], tries:
    ↪ int) -> float:
    """Return an approximation for pi.

    >>> from math import pi
    >>> from random import seed
    >>> seed(7897) # Tests should be reproducible
    >>> within_circle = lambda x, y: x**2 + y**2 < 1
    >>> abs(4*approx_fun(within_circle, 1000) - pi) < 10e-2
    True
    """

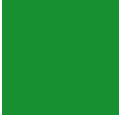
    assert tries > 0
    true_cases = 0
    for i in range(0, tries):
        x = random() # range [0,1)
        y = random()
        if predicate(x, y):
            true_cases += 1
    return true_cases / tries
```

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Random number are useful also for *simulation*: for example, we could simulate **evolutionary drift**.

```
from random import seed, randint, getstate, setstate

class DriftSimulation:
    def __init__(self, sim_seed: int = 232943) -> None:
        self.population = ['\N{MONKEY}', '\N{TIGER}', '\N{BUTTERFLY}', '\N{LIZARD}',
        ↪ '\N{SNAIL}']
        seed(sim_seed)
        self.r_state = getstate()

    def offspring(self) -> None:
        setstate(self.r_state)
        new = self.population[randint(0, len(self.population)-1)]
        self.population[randint(0, len(self.population)-1)] = new
        self.r_state = getstate()

    def simulate(self, generations: int) -> None:
        for i in range(0, generations):
            self.offspring()

a = DriftSimulation()
b = DriftSimulation()
a.simulate(2)
b.simulate(2)
```