



PyQB

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Abstracting
similaritiesProcedural
encapsulation

Programming in Python¹

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Lecture IX: Working with abstractions

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Status of the homework

	accepted	done
One triangle	19	10
Triangle kinds	14	5
Newton square root	10	4
Pythagorean triplets	15	7
Sonar	13	3

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List slices

- List slicing is a powerful feature in Python that allows you to create a new list by extracting a portion of an existing list.
- It's like cutting out a piece of a list you specify the starting and ending indices (exclusive of the end index).
- Syntax: `mylist[start:end]`
- `start` (optional): The index where the slice begins (inclusive). Defaults to 0.
- `end` (optional): The index where the slice ends (exclusive). Defaults to the end of the list.

'a'	'b'	'c'	'd'	'e'
0	1	2	3	4

`mylist[1:4]`

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Examples



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```
my_list = [0, 1, 2, 3, 4, 5, 6, 7, 8, 9]

# Slice from index 2 to 5 (exclusive):
slice1 = my_list[2:5] # [2, 3, 4]

# Slice from the beginning to index 3 (exclusive):
slice2 = my_list[:3] # [0, 1, 2]

# Slice from index 6 to the end:
slice3 = my_list[6:] # [6, 7, 8, 9]

# Create a copy of the entire list:
slice4 = my_list[:] # [0, 1, 2, 3, 4, 5, 6, 7, 8, 9]
```

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More slicing



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```
my_list = [0, 1, 2, 3, 4, 5, 6, 7, 8, 9]
```

- **Step Size:** You can add a third argument to specify a step size (e.g., `mylist[start:end:step]`). `my_list[1:8:2]` creates a slice starting at index 1, going up to (but not including) index 8, with a step size of 2. `[1, 3, 5, 7]`
- **Negative Indices:** Indices can be negative, counting from the end of the list. `-1` is the last element, `-2` is the second to last, etc. `my_list[-3:]` takes the last three elements of the list. `[7, 8, 9]`; `my_list[:-1]` gets all elements except the last.

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A slice is always a new object



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```
x = [100, 200, 300, 400, 500]

slice = x[1:4]

slice[0] = 666

print(f'{x=} {slice=}')

# x=[100, 200, 300, 400, 500] slice=[666, 300, 400]
```

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Procedural abstraction



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Procedural abstraction is key for our thinking process (remember the power of recursion, for example): giving a name to a procedure/function enhances our problem solving skills.

```
def sum_range(a: int, b: int) -> int:
    """Sum integers from a through b.

    >>> sum_range(1, 4)
    10

    >>> sum_range(3, 3)
    3
    """
    assert b >= a
    result = 0
    for i in range(a, b+1):
        result = result + i
    return result
```

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Another “sum”



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This is very similar...

```
def sum_range_cubes(a: int, b: int) -> int:
    """Sum the cubes of the integers from a through b.

    >>> sum_range_cubes(1, 3)
    36

    >>> sum_range_cubes(-2, 2)
    0

    """
    assert b >= a
    result = 0
    for i in range(a, b+1):
        result = result + cube(i) # cube(i: int) -> int
        ↪ defined elsewhere
    return result
```

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Another “sum”



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This is also very similar...

$$\frac{1}{a \cdot (a+2)} + \frac{1}{(a+4) \cdot (a+6)} + \frac{1}{(a+8) \cdot (a+10)} + \dots + \frac{1}{(b-2) \cdot (b)}$$

$$(\text{Leibniz: } \frac{1}{1 \cdot 3} + \frac{1}{5 \cdot 7} + \frac{1}{9 \cdot 11} + \dots = \frac{\pi}{8})$$

```
def pi_sum(a: int, b: int) -> float:
    """Sum 1/(a(a+2)) terms until (a+2) > b.

    >>> from math import pi
    >>> abs(8*pi_sum(1, 1001) - pi) < 10e-3
    True

    """
    assert b >= a
    result = 0.0
    for i in range(a, b+1, 4):
        result = result + (1 / (i * (i + 2)))
    return result
```

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Can we abstract the similarity?



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```
from collections.abc import Callable

Num = int | float

def gen_sum(a: int, b: int, fun: Callable[[int], Num], step: int = 1) -> Num:
    """Sum terms from a through b, incrementing by step.

    >>> gen_sum(1, 4, lambda x: x)
    10

    >>> gen_sum(1, 3, lambda x: x**3)
    36

    >>> from math import pi
    >>> abs(8*gen_sum(1, 1000, lambda x: 1 / (x * (x + 2))), 4) - pi < 10e-3
    True

    """
    assert b >= a
    result = 0.0
    for i in range(a, b+1, step):
        result = result + fun(i)
    if isinstance(result, float) and result.is_integer():
        return int(result)
    return result
```

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The huge value of procedural abstraction



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It is worth to emphasize again the huge value brought by **procedural abstraction**. In Python it is not mandatory to use procedures/functions: the language is designed to be used also for *on the fly* calculations.

```
x = 45
s = 0
for i in range(0, x):
    s = s + i
```

- the piece of functionality is not easily to distinguish it could be intertwined with other unrelated code

- the goal is not explicit, which data are needed, what computes
- it's hard to reuse even in slightly different contexts

This is ok, but it is not encapsulated (in fact, since encapsulation is so important you can at least consider it encapsulated in file which contains it)

```
x = 45
a = 67 # another concern
s = 0
for i in range(0, x):
    s = s + i
print(a) # another concern
```

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Encapsulate the functionality



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```
def sum_to(x: int) -> int:
    assert x >= 0
    r = 0
    for i in range(0, x):
        r = r + i
    return r
```

```
s = sum_to(45)
```

- It gives to our mind a “piece of functionality”, the interpreter we are programming is now “able” to do a new thing that can be used **without thinking about the internal details**
- It makes clear which data it needs (an integer, ≥ 0 if we add also an assertion or a docstring)
- It makes clear that the interesting result is another integer produced by the calculation
- It can be reused easily and safely

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Homework



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- <https://classroom.github.com/a/Auwejr2m>

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