



PyQB

Monga

Functions

# Programming in Python<sup>1</sup>

Mattia Monga

Dip. di Informatica  
Università degli Studi di Milano, Italia

`mattia.monga@unimi.it`

Academic year 2021/22, II semester



PyQB

Monga

Functions

# Lecture IV: Functions



## In Python3

- Variables are names to refer to objects;
- Objects are elements of types, which define the operations that make sense on them;
- Therefore, the basic instructions are the **assignment** (bind a name to an object), **the proper operations for each object**, and the **commands** to ask the services of the operating system;
- One can alter the otherwise strictly sequential execution of instruction with control flow statements: **if**, **for**, **while**.

Remember that in python3, indentation matters (it is part of the syntax).



PyQB

Monga

Functions

- Solve “One Triangle” on CS Circles
- Submit your solution via github  
<https://classroom.github.com/a/Itfv06Jy>



# Proper operations

- On objects one can apply **binary** and **unary** operators: `2 * 3 - (-5.0) not True 'foo' + 'bar'...`
- There also **built-in** functions like `max(8,5,6)`, the full list is here: <https://docs.python.org/3/library/functions.html>
- (syntactically, commands like `print` or `input` cannot be distinguished from other built-in functions)
- Every object has methods that can be applied with the so called **dot notation**: `(3.2).is_integer()` `'foo'.upper()` `'xxx'.startswith('z')`; the list of which methods an object has is given by `dir(object)`.

PyQB

Monga

Functions





# Definition of functions

As variables are names for objects, one can also name fragments of code:

```
def cube(x: int) -> int:  
    square = x * x  
    return square * x
```

Now we have a new operation `cube`, acting on `ints`: `cube(3)`. Type hints are optional (and ignored, you can call `cube(3.2)` or `cube('foo')`), but **very useful** for humans (and tools like `mypy`).

*# Equivalent*

```
def cube(x):  
    square = x * x  
    return square * x
```

PyQB

Monga

Functions



# A function computes a result

- Returns a useful result

```
def concat_with_a_space(string1, string2):  
    return string1 + ' ' + string2
```

```
# string1 is the _formal_ parameter  
# 'foo' is the _actual_ parameter (like an assignment string1 =  
↪ 'foo')  
print(concat_with_a_space('foo', 'bar'))
```

- Return None

```
def repeated_print(string, repetitions):  
    for i in range(0, repetitions):  
        print(string)
```

```
repeatedPrint('Hello, world!', 3)
```

- Recursive call:

```
def repeatedPrint(string, repetitions):  
    if repetitions > 0:  
        print(string)  
        repeatedPrint(string, repetitions - 1)
```

```
repeatedPrint('Hello, world!', 3)
```

PyQB

Monga

Functions



# Functions are objects too

One can assign functions to variables:

```
def cube(x: int) -> int:  
    square = x * x  
    return square * x
```

```
mycube = cube
```

```
print(mycube(3))  
print(type(mycube))
```

And short functions can even be expressed as literal expressions  
(lambda expressions)

```
cube = lambda y: y*y*y
```

PyQB

Monga

Functions





# Naming helps solving



PyQB

Monga

Functions

The tower of Hanoi

<https://www.mathsisfun.com/games/towerofhanoi.html>



# Describe the moves for a solution

Recursive thinking is a powerful problem solving technique and it can be translated to Python thanks to recursive calls.

Hanoi moves  $A \rightarrow C$ :

- In  $A$  there is just one disk: move it to  $C$
- Otherwise in  $A$  there are  $n$  disks ( $> 1$ ):
  - **leap of faith!** I suppose to know the moves needed to move  $n - 1$  disk; then
    - apply this (supposed) solution to move  $n - 1$  disks from  $A$  to  $B$  (leveraging on  $C$ , empty, as the third pole)
    - move the last disk from  $A$  to  $C$
    - apply the (supposed) solution to move  $n - 1$  disks from  $B$  to  $C$  (leveraging on  $A$ , now empty, as the third pole)

This implicit description solve the problem! Finding a non-recursive solution is possible but not that easy.

PyQB

Monga

Functions



```
def hanoi(n: int, a_from: str, c_to: str,  
↪ b_intermediate: str):  
    if n == 1:  
        print('Move 1 disk from ' + a_from + ' to ' + c_to)  
        return  
    hanoi(n - 1, a_from, b_intermediate, c_to)  
    print('Move 1 disk from ' + a_from + ' to ' + c_to)  
    hanoi(n - 1, b_intermediate, c_to, a_from)
```

```
hanoi(3, 'A', 'C', 'B')
```



PyQB

Monga

Functions

- Chapters 7A, 10, 11A, 11B, 11C, 12
- Create an account on <https://github.com/> (if you don't have one) and send me the name (Zulip preferred, use a private message if you don't want to make it known to the other students).