



PyQB

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Functions

Programming in Python¹

Mattia Monga

Dip. di Informatica
Università degli Studi di Milano, Italia

`mattia.monga@unimi.it`

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Lecture III: Functions and lists

International Women's Day



Ada Byron (Lady King, Countess of Lovelace, 1815–1852) wrote the first ever program for an automatic machine, the “analytical engine” designed (but never built) by Charles Babbage.

In 1840, C. Babbage gave a seminar in Turin, Luigi Menabrea (future Italian prime minister) transcribed it into French, Ada translated it to English. . . with many original notes, and a program to compute Bernoulli numbers (1843).

An important programming language was named after her: Ada.



Daguerreotype by
Antoine Claudet,
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In Python3

- Variables are names to refer to objects;
- Objects are elements of types, which define the operations that make sense on them;
- Therefore, the basic instructions are the **assignment** (bind a name to an object), **the proper operations for each object**, and the **commands** to ask the services of the operating system;
- One can alter the otherwise strictly sequential execution of instruction with control flow statements: **if**, **for**, **while**.

Remember that in python3, indentation matters (it is part of the syntax).



Proper operations

- On objects one can apply **binary** and **unary** operators: `2 * 3 - (-5.0) not True 'foo' + 'bar'...`
- There also **built-in** functions like `max(8,5,6)`, the full list is here: <https://docs.python.org/3/library/functions.html>
- (syntactically, commands like `print` or `input` cannot be distinguished from other built-in functions)
- Every object has methods that can be applied with the so called **dot notation**: `(3.2).is_integer()` `'foo'.upper()` `'xxx'.startswith('z')`; the list of which methods an object has is given by `dir(object)`.

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Definition of functions

As variables are names for objects, one can also name fragments of code:

```
def cube(x: int) -> int:  
    square = x * x  
    return square * x
```

Now we have a new operation `cube`, acting on `ints`: `cube(3)`. Type hints are optional (and ignored, you can call `cube(3.2)` or `cube('foo')`), but **very useful** for humans (and tools like `mypy`).

Equivalent

```
def cube(x):  
    square = x * x  
    return square * x
```

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A function computes a result

- Returns a useful result

```
def concat_with_a_space(string1, string2):  
    return string1 + ' ' + string2
```

```
# string1 is the _formal_ parameter  
# 'foo' is the _actual_ parameter (like an assignment string1 =  
↪ 'foo')
```

```
print(concat_with_a_space('foo', 'bar'))
```

- Return None

```
def repeated_print(string, repetitions):  
    for i in range(0, repetitions):  
        print(string)
```

```
repeatedPrint('Hello, world!', 3)
```

- Recursive call:

```
def repeatedPrint(string, repetitions):  
    if repetitions > 0:  
        print(string)  
        repeatedPrint(string, repetitions - 1)
```

```
repeatedPrint('Hello, world!', 3)
```



Functions are objects too

One can assign functions to variables:

```
def cube(x: int) -> int:  
    square = x * x  
    return square * x
```

```
mycube = cube
```

```
print(mycube(3))  
print(type(mycube))
```

And short functions can even be expressed as literal expressions
(lambda expressions)

```
cube = lambda y: y*y*y
```

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Naming helps solving



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The tower of Hanoi

<https://www.mathsisfun.com/games/towerofhanoi.html>



Describe the moves for a solution

Recursive thinking is a powerful problem solving technique and it can be translated to Python thanks to recursive calls.

Hanoi moves $A \rightarrow C$:

- In A there is just one disk: move it to C
- Otherwise in A there are n disks (> 1):
 - **leap of faith!** I suppose to know the moves needed to move $n - 1$ disk; then
 - apply this (supposed) solution to move $n - 1$ disks from A to B (leveraging on C , empty, as the third pole)
 - move the last disk from A to C
 - apply the (supposed) solution to move $n - 1$ disks from B to C (leveraging on A , now empty, as the third pole)

This implicit description solve the problem! Finding a non-recursive solution is possible but not that easy.

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```
def hanoi(n: int, a_from: str, c_to: str,  
↪ b_intermediate: str):  
    if n == 1:  
        print('Move 1 disk from ' + a_from + ' to ' + c_to)  
        return  
    hanoi(n - 1, a_from, b_intermediate, c_to)  
    print('Move 1 disk from ' + a_from + ' to ' + c_to)  
    hanoi(n - 1, b_intermediate, c_to, a_from)
```

```
hanoi(3, 'A', 'C', 'B')
```



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- Chapters 7A, 10, 11A, 11B, 11C, 12
- Create an account on <https://github.com/> (if you don't have one) and send me the name (Zulip preferred, use a private message if you don't want to make it known to the other students).