



PyQB

Monga

Functions

Programming in Python¹

Mattia Monga

Dip. di Informatica
Università degli Studi di Milano, Italia
mattia.monga@unimi.it

Academic year 2020/21, II semester

¹ © 2020 M. Monga. Creative Commons Attribution — Condividi allo stesso modo 4.0 Internazionale. <http://creativecommons.org/licenses/by-sa/4.0/deed.it>



PyQB

Monga

Functions

Lecture III: Functions and lists



PyQB

Monga

Functions

International Women's Day

Ada Byron (Lady King, Countess of Lovelace, 1815–1852) wrote the first ever program for an automatic machine, the “analytical engine” designed (but never built) by Charles Babbage.

In 1840, C. Babbage gave a seminar in Turin, Luigi Menabrea (future Italian prime minister) transcribed it into French, Ada translated it to English. . . with many original notes, and a program to compute Bernoulli numbers (1843).

An important programming language was named after her: Ada.



Daguerreotype by Antoine Claudet, public domain



PyQB

Monga

Functions

Summary

In Python3

- Variables are names to refer to objects;
- Objects are elements of types, which define the operations that make sense on them;
- Therefore, the basic instructions are the assignment (bind a name to an object), the proper operations for each object, and the commands to ask the services of the operating system;
- One can alter the otherwise strictly sequential execution of instruction with control flow statements: `if`, `for`, `while`.

Remember that in python3, indentation matters (it is part of the syntax).

Proper operations



PyQB

Monga

Functions

- On objects one can apply binary and unary operators: `2 * 3` `-(-5.0)` `not True` `'foo' + 'bar'...`
- There also built-in functions like `max(8,5,6)`, the full list is here: <https://docs.python.org/3/library/functions.html>
- (syntactically, commands like `print` or `input` cannot be distinguished from other built-in functions)
- Every object has methods that can be applied with the so called **dot notation**: `(3.2).is_integer()` `'foo'.upper()` `'xxx'.startswith('z')`; the list of which methods an object has is given by `dir(object)`.

28

Definition of functions



PyQB

Monga

Functions

As variables are names for objects, one can also name fragments of code:

```
def cube(x: int) -> int:
    square = x * x
    return square * x
```

Now we have a new operation `cube`, acting on `ints`: `cube(3)`. Type hints are optional (and ignored, you can call `cube(3.2)` or `cube('foo')`), but **very useful** for humans (and tools like `mypy`).

```
# Equivalent
def cube(x):
    square = x * x
    return square * x
```

29

A function computes a result



PyQB

Monga

Functions

- Returns a useful result

```
def concat_with_a_space(string1, string2):
    return string1 + ' ' + string2
```

```
# string1 is the _formal_ parameter
# 'foo' is the _actual_ parameter (like an assignment string1 =
# ↪ 'foo')
print(concat_with_a_space('foo', 'bar'))
```

- Return None

```
def repeated_print(string, repetitions):
    for i in range(0, repetitions):
        print(string)
```

```
repeatedPrint('Hello, world!', 3)
```

- Recursive call:

```
def repeatedPrint(string, repetitions):
    if repetitions > 0:
        print(string)
        repeatedPrint(string, repetitions - 1)
```

```
repeatedPrint('Hello, world!', 3)
```

30

Functions are objects too



PyQB

Monga

Functions

One can assign functions to variables:

```
def cube(x: int) -> int:
    square = x * x
    return square * x
```

```
mycube = cube
```

```
print(mycube(3))
print(type(mycube))
```

And short functions can even be expressed as literal expressions (lambda expressions)

```
cube = lambda y: y*y*y
```

31

Naming helps solving



PyQB

Monga

Functions

The tower of Hanoi

<https://www.mathsisfun.com/games/towerofhanoi.html>

32

Describe the moves for a solution



PyQB

Monga

Functions

Recursive thinking is a powerful problem solving technique and it can be translated to Python thanks to recursive calls.

Hanoi moves $A \rightarrow C$:

- In A there is just one disk: move it to C
- Otherwise in A there are n disks (> 1):
 - **leap of faith!** I suppose to know the moves needed to move $n - 1$ disk; then
 - apply this (supposed) solution to move $n - 1$ disks from A to B (leveraging on C , empty, as the third pole)
 - move the last disk from A to C
 - apply the (supposed) solution to move $n - 1$ disks from B to C (leveraging on A , now empty, as the third pole)

This implicit description solve the problem! Finding a non-recursive solution is possible but not that easy.

33

In Python



PyQB

Monga

Functions

```
def hanoi(n: int, a_from: str, c_to: str,
        ↪ b_intermediate: str):
    if n == 1:
        print('Move 1 disk from ' + a_from + ' to ' + c_to)
        return
    hanoi(n - 1, a_from, b_intermediate, c_to)
    print('Move 1 disk from ' + a_from + ' to ' + c_to)
    hanoi(n - 1, b_intermediate, c_to, a_from)
```

```
hanoi(3, 'A', 'C', 'B')
```

34

Homework



PyQB

Monga

Functions

- Chapters 7A, 10, 11A, 11B, 11C, 12
- Create an account on <https://github.com/> (if you don't have one) and send me the name (Zulip preferred, use a private message if you don't want to make it known to the other students).

35