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# Programming in Python<sup>1</sup>

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Academic year 2020/21, II semester

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# Lecture I: Programming in Python for quantitative biologists

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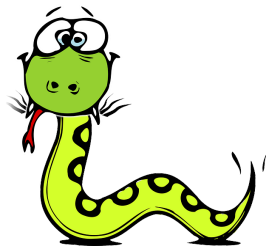
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# Programming in Python (for quantitative biologists)



The course introduces imperative programming by referring to the Python language.

- 1 Python3 and its object-oriented features;
- 2 Python3 libraries that can be useful in scientific computation and data analysis, in particular NumPy and pandas.



Everything will be available on:

[mattiamon.ga/pyqb](https://mattiamon.ga/pyqb)

(a.k.a. <https://mamelio.docenti.di.unimi.it/pyqb>)

Please: fill in the survey, subscribe to Zulip.

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# Course schedule



- Mondays, Fridays 9:30–11:30 (am)
- Lectures: 40h (online), Labs: 16h (face-to-face if possible)
- Labs always on Friday, 12/3 19/3 9/4 23/4 7/5 21/5 4/6 11/6
- We will explore different setups: (1) a “scaffolded” one for the first steps, (2) the plain python interpreter, and finally (3) the notebooks popular in scientific practice
- Tutor: dott. Davide Paolillo (computer science master student)
- Text: every Python3 reference/book/tutorial is ok, you can access freely to the book linked on the website
- Final test: write (small) python programs without help

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# Why Python?



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Programming can be approached in many “languages”, the fundamental skills are general. . . but you cannot learn without referring to a specific language.

- A precise requirement of the teaching committee
- Very popular in the scientific landscape
- Easy to learn, many useful libraries, free software
- Alternatives: Fortran, C, Matlab, Mathematica, R, Julia, . . .
- Python is slower, but it is considered easier to understand and manage

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# Which Python?



We will use Python3 (current version is 3.9): be careful when looking around, Python2 is still very common (but deprecated) and incompatible. Python supports different “paradigms”, we will focus on:

- Imperative programming: programs describe **changes** in *registers* and the *executing environment*;
- Object-oriented: complex (imperative) programs are organized around **objects** in order to hide and isolate complexity.

This is a **programming course**: I will try to propose example that I believe could be useful in your daily practice, but I'm not a biologist.

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Programming in science can serve two (almost opposite) goals:

- 1 Understanding every detail of a computational process;
- 2 Compose computational process by assembling powerful build blocks of which you understand very little.

Most of the current popularity of programming is related to goal 2... with many *sorcerer's apprentices*. But this course will focus mainly on goal 1. In the last part of the course we will bend towards 2, hopefully with a solid background.

Programming can be both hard and addictive: **Teach Yourself Programming in Ten Years**

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# Fundamental concepts of Python



The programmer describes computational processes in terms of:

**objects** : all the entities manipulated by the program, each has an **identity** (can be distinguished) and a **value**, that is an element in a specific **type** (a set of values together with the operations that make sense on them)

**basic types** : integers (**int**), floats, strings (**str**), functions; they can be composed in more complex types

**variables** : **names** used to refer to objects; the same name can refer to different objects during the same process

**special commands** : the only way to change the execution environment (i.e., the “virtual machine” provided by the operating system) is to use **system calls**; syscalls change from system to system (e.g., Linux vs. Windows), but Python wraps them and they appear like the functions written by the programmers (e.g., **print**), even if they could not be programmed in Python.

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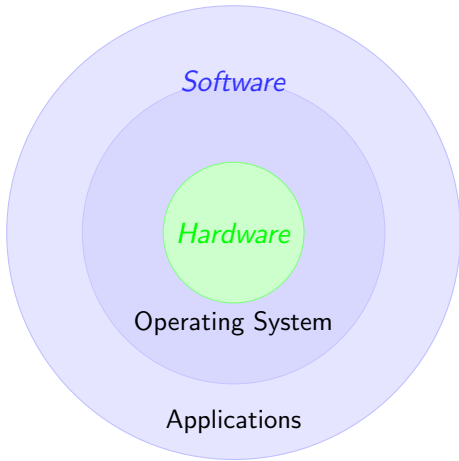
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# The onion model



- Operating System: it is the only program interpreted directly by the hardware; other pieces of software get interpreted by the virtual machine provided by it.
- Applications: programs (e.g., the python interpreter or python programs) executed within the protected environment created by the operating system.

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# Let's try!



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<https://python.di.unimi.it/>

You can use it without any personal account, but if you want support you must create one, putting me as the “guru”: `mmonga`

This platform will be used for the first lessons, since it requires no setup at all: everything happens in the browser (and the server).

(Thanks to the University of Waterloo, Canada for providing the CS Circles)

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# Assignment



This is the fundamental statement for imperative programming:

- A **name**, known as **variable**, is needed to refer to objects.  
`professor = "Mattia"`
- = **is not symmetrical**, read it as **becomes**: Left-hand-side is always a variable, right-hand-side is an object, that can be either a **literal** or anything referred by another variable.

- A variable can change its value with another, following, assignment. Thus, the same variable may refer to different objects.

```
professor = "Violetta"
```

- Basic objects (numbers, strings, Boolean values) are **immutable** (the variable change, not the object; different objects have always different identity)
- **Tracking** a program means to track the values of all the variables of a program during its execution.

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# Basic operations



- **Binary operators:**  $5 + 2$ , they compute a new object by using the two objects on which they apply;
- **Unary operators:**  $-(-5)$ ;
- **Functions:** `max`, they compute a new object by using an arbitrary number of objects (in general  $0 \dots$ , `max` takes at least 1) **passed** as **parameters** (or **arguments**) when the function is **called** (`max(3, 6, something_else)`); sometimes the object computed is `None`;
- Syntactically appear as functions, but *commands* like `print("Hello!")` are actually used to request **side effects** in the executing environment.

[Documentazione ufficiale di Python \(3.9\)](#)

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# Different approaches



Problem: exchange the name of two objects (Chapter 1, last exercise).

- Know the basic syntax of **variables** and **assignment** =
- Know the semantics of what you write: assigning an object to a variable delete any previous assignment;

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# Different approaches



Problem: exchange the name of two objects (Chapter 1, last exercise).

- Know the basic syntax of **variables** and **assignment** =
- Know the semantics of what you write: assigning an object to a variable delete any previous assignment;
- Natural strategy: use a temporary name to “save” the value during the exchange;

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# Different approaches



Problem: exchange the name of two objects (Chapter 1, last exercise).

- Know the basic syntax of **variables** and **assignment** =
- Know the semantics of what you write: assigning an object to a variable delete any previous assignment;
- Natural strategy: use a temporary name to “save” the value during the exchange;
- “Fox” strategy: know language or library tricks For example Python has a “multiple assignment” construct  $x, y = y, x$ , or a special library function `swap(x, y)` could exist;

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# Different approaches



Problem: exchange the name of two objects (Chapter 1, last exercise).

- Know the basic syntax of **variables** and **assignment** =
- Know the semantics of what you write: assigning an object to a variable delete any previous assignment;
- Natural strategy: use a temporary name to “save” the value during the exchange;
- “Fox” strategy: know language or library tricks For example Python has a “multiple assignment” construct  $x, y = y, x$ , or a special library function `swap(x, y)` could exist;
- “Hedgehog” strategy: study the problem in depth, e.g., if objects are numbers you can exploit arithmetic.

$$x = x + y$$
$$y = x - y$$
$$x = x - y$$

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Finish chapters 1, 1E, 2, 2X, 3, 4.

It shouldn't take more than three hours (one hour per day...),  
but exercising is **crucial**.



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# Lecture II: Control structures

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To answer the questions I will rise please connect to:

[sli.do](https://sli.do) Event#: 57146

(MS Teams: a tab in the channel is already set on that)

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# Summary



- Programming means to instruct an (automatic) interpreter with a precise description of a computational process.
- (In fact, the only way to make a description precise is to specify exactly the interpreter)
- We use a software interpreter, itself a program interpreted by the operating system (the stack of interpreters can be much deeper).
- Our interpreter (Python3) manipulates objects taken from types (that define which manipulations are possible), referred by variables, with special commands to ask the services provided by the operating system.

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# Basic types



`bool` `False`, `True` Logical operations

`int` 1, -33, 1\_000\_000\_000 ... Arithmetic operations, no upper or lower limit

`float` 1.0, .1, 1.2e34 ... Arithmetic operations, limited but you have `float('infinity')` (and `float('nan')`)

```
sys.float_info(max=1.7976931348623157e+308,
               ↪ , max_exp=1024, max_10_exp=308,
               ↪ min=2.2250738585072014e-308,
               ↪ min_exp=-1021, min_10_exp=-307,
               ↪ dig=15, mant_dig=53,
               ↪ epsilon=2.220446049250313e-16,
               ↪ radix=2, rounds=1)
```

`str` `'aaa\nthis is on a new line'`,  
`"bbb'b\"b"` ... Concatenation, alphabetical ordering, replication, ...

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# Sequence of operations



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```
1 x = 1 + 2 * 3
2 x = x + 1
```

The 2 lines of code translate to at least 5 “logical” instructions (maybe more, for example adding two big numbers require multiple instructions):

- 1  $2 * 3$
- 2  $1 + 6$
- 3  $x = 7$
- 4  $7 + 1$
- 5  $x = 8$

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# Flow of control

It is normally not very useful to write programs that do just one single computation. You wouldn't teach a kid how to multiply  $32 \times 43$ , but the **general algorithm** of multiplication (the level of generality can vary).

To write programs that address a family of problems we need to be able to **select** instructions to execute according to **conditions**.

```
if x < 0:
    x = -x
y = 2 * x

if x == -1:
    x = x + 1
else:
    x = 3 * x
y = 2 * x
```

In Python the indentation is part of the syntax and it is **mandatory**.

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# Repetitions



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It is also useful to be able to **repeat** instructions: it is very convenient, but it also opens a deep Pandora's box. . .

There are two ways of **looping** in Python:

Repeat by iterating on the elements of a collection (similar to math notation

$$\sum_{i \in \{a,b,c\}} f(i)$$

```
for i in range(0, 5):  
    # 0 1 2 3 4  
    print(i)
```

Repeat while a (variable) condition is true

```
i = 0  
while i < 5:  
    print(i)  
    i = i + 1
```

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# Loops can be difficult to understand



When you have loops, understanding the code can be a difficult task and the only general strategy is to track the execution.

*# This is known as Collatz's procedure*

```
n = ...
```

```
while n > 1:
```

```
    if n % 2 == 0:
```

```
        # if the remainder of division by 2 is 0, i.e. n
```

```
        ↪ is even
```

```
        n = n / 2
```

```
    else:
```

```
        n = 3*n + 1
```

We know (by empirical evidence) that it ends for all  $n < 2^{68} \approx 10^{20}$ , nobody is able to predict the number of iterations given any  $n$ .

With loops it is also hard to exploit parallel execution.

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# Learn to write loops can be hard



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When you write a loop, you should have in mind two related goals:

- 1 **the loop must terminate**: this is normally easy with **for** loops (when the finite collection ends, the loop ends also), but it can be tricky with **while**s (remember to change something in the condition);
- 2 **the loop repeats something**: the programmer should be able to write the “repeating thing” in a way that makes it equal in its form (but probably different in what it does).

The second part (technically known as **loop invariant**) is the hardest to learn, since it requires experience, creativity, and ingenuity.

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CS Circles chapters 6, 7C, and 9.



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# Lecture III: Functions and lists

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# International Women's Day



**Ada Byron** (Lady King, Countess of Lovelace, 1815–1852) wrote the first ever program for an automatic machine, the “analytical engine” designed (but never built) by Charles Babbage.

In 1840, C. Babbage gave a seminar in Turin, Luigi Menabrea (future Italian prime minister) transcribed it into French, Ada translated it to English. . . with many original notes, and a program to compute Bernoulli numbers (1843).

An important programming language was named after her: Ada.



Daguerreotype by Antoine Claudet, public domain

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# Summary



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## In Python3

- Variables are names to refer to objects;
- Objects are elements of types, which define the operations that make sense on them;
- Therefore, the basic instructions are the **assignment** (bind a name to an object), **the proper operations for each object**, and the **commands** to ask the services of the operating system;
- One can alter the otherwise strictly sequential execution of instruction with control flow statements: **if**, **for**, **while**.

Remember that in python3, indentation matters (it is part of the syntax).

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# Proper operations



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- On objects one can apply **binary** and **unary** operators: `2 * 3 - (-5.0) not True 'foo' + 'bar'...`
- There also **built-in** functions like `max(8,5,6)`, the full list is here: <https://docs.python.org/3/library/functions.html>
- (syntactically, commands like `print` or `input` cannot be distinguished from other built-in functions)
- Every object has methods that can be applied with the so called **dot notation**: `(3.2).is_integer()` `'foo'.upper()` `'xxx'.startswith('z')`; the list of which methods an object has is given by `dir(object)`.

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# Definition of functions

As variables are names for objects, one can also name fragments of code:

```
def cube(x: int) -> int:
    square = x * x
    return square * x
```

Now we have a new operation `cube`, acting on `ints`: `cube(3)`. Type hints are optional (and ignored, you can call `cube(3.2)` or `cube('foo')`), but **very useful** for humans (and tools like `mypy`).

*# Equivalent*

```
def cube(x):
    square = x * x
    return square * x
```

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# A function computes a result



- Returns a useful result

```
def concat_with_a_space(string1, string2):  
    return string1 + ' ' + string2
```

```
# string1 is the _formal_ parameter  
# 'foo' is the _actual_ parameter (like an assignment string1 =  
↪ 'foo')
```

```
print(concat_with_a_space('foo', 'bar'))
```

- Return None

```
def repeated_print(string, repetitions):  
    for i in range(0, repetitions):  
        print(string)
```

```
repeatedPrint('Hello, world!', 3)
```

- Recursive call:

```
def repeatedPrint(string, repetitions):  
    if repetitions > 0:  
        print(string)  
        repeatedPrint(string, repetitions - 1)
```

```
repeatedPrint('Hello, world!', 3)
```

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# Functions are objects too



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One can assign functions to variables:

```
def cube(x: int) -> int:  
    square = x * x  
    return square * x
```

```
mycube = cube
```

```
print(mycube(3))  
print(type(mycube))
```

And short functions can even be expressed as literal expressions  
(lambda expressions)

```
cube = lambda y: y*y*y
```

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# Naming helps solving



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The tower of Hanoi

<https://www.mathsisfun.com/games/towerofhanoi.html>

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# Describe the moves for a solution



Recursive thinking is a powerful problem solving technique and it can be translated to Python thanks to recursive calls.

Hanoi moves  $A \rightarrow C$ :

- In  $A$  there is just one disk: move it to  $C$
- Otherwise in  $A$  there are  $n$  disks ( $> 1$ ):
  - **leap of faith!** I suppose to know the moves needed to move  $n - 1$  disk; then
    - apply this (supposed) solution to move  $n - 1$  disks from  $A$  to  $B$  (leveraging on  $C$ , empty, as the third pole)
    - move the last disk from  $A$  to  $C$
    - apply the (supposed) solution to move  $n - 1$  disks from  $B$  to  $C$  (leveraging on  $A$ , now empty, as the third pole)

This implicit description solve the problem! Finding a non-recursive solution is possible but not that easy.

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# In Python



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```
def hanoi(n: int, a_from: str, c_to: str,
↪ b_intermediate: str):
    if n == 1:
        print('Move 1 disk from ' + a_from + ' to ' + c_to)
        return
    hanoi(n - 1, a_from, b_intermediate, c_to)
    print('Move 1 disk from ' + a_from + ' to ' + c_to)
    hanoi(n - 1, b_intermediate, c_to, a_from)

hanoi(3, 'A', 'C', 'B')
```

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- Chapters 7A, 10, 11A, 11B, 11C, 12
- Create an account on <https://github.com/> (if you don't have one) and send me the name (Zulip preferred, use a private message if you don't want to make it known to the other students).

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# Lecture IV: Using the “naked” interpreter

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# The pieces of software



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- Python 3.9.2, with pip and the IDLE editor (on MS Windows they are bundled together):  
<https://www.python.org/downloads/>
- Git 2.30.2: <https://git-scm.com/downloads>
- (optional, Win and Mac only) Github desktop  
<https://desktop.github.com/>

Homework assignments will be available via Github Classroom (you will need a Github account). For example:

<https://classroom.github.com/a/TpWhD1zt>

When you **push** (hand in) your solution, a suite of tests is run.

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# Software Configuration Management



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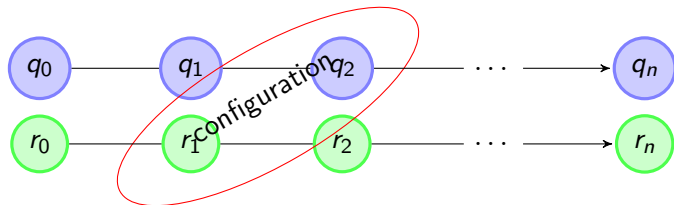
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Software Configuration Management like `git` are tools designed to track all the **revisions** of some set of software **artifacts** (files).



The system configuration itself evolves in different **versions**. One can have multiple **branches** of evolution.

A motivating talk on why you should use tools like these in your scientific work.



git is a powerful tool to manage all this complexity in a very efficient (and distributed) way. It is not an easy tool, however. A good tutorial is [here](#). But for this course we use a very simplistic workflow:

- 1 Clone (copy) on your machine a repository `git clone ...`;
- 2 Work on the artifacts
- 3 Add the modified artifacts to the changeset you want to “publish” `git add ...`
- 4 Commit the changeset `git commit -m"message"` providing a comment about what have you done
- 5 Push the changeset on Github `git push`
- 6 (If someone else is working on the same artifacts you can sync with `git pull`)

All these steps are very easy (almost hidden, especially authentication) if you use Github desktop.

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**Programs are data!** File extension is conventionally `.py`

- To edit Python programs you need a **text editor**: something like Notepad, not Word (a word processor)
- IDLE is the “standard” one provided by the Python distribution itself: it is easy to use and it provides an easy way for executing programs without getting to the command line
- Other good choices: VS Code Atom Notepad++ or any other universal text editor like EMACS or vi

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# Lecture V: Composite objects

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- Students list has 26 names...
- ...but only 18 accepted the assignment on GitHub Classroom
- (12 students pushed a correct solution)

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# Simple and composite objects



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- **ints** **floats** **bools** are simple objects: they have no “parts”
- Strings are an example of composite objects since it is possible to consider also the characters: a **str** is a sequence of single characters; an important (simplifying) property: they are **immutable**
- Generic **immutable** sequences (with elements of any type) are called **tuples** (**tuple**): (1, 2, 'foo') (1,)
- Generic **mutable** sequences (with elements of any type) are called **lists** (**list**): [1, 2, 'foo'] [1]  
[1,2].append(3)

# Mutability



Immutable objects are simpler to use:

```
x = (1, 2, 3)
y = x
```

```
x = (10, 20, 30) # x refers to a new object, since the
                 ↪ old cannot be changed
```

```
print(x, y)
```

Mutable ones require some caution:

```
x = [1, 2, 3]
y = x
```

```
x[0] = 10 # both x and y refer to a changed object
print(x, y)
```

```
x = [100, 200, 300]
print(x, y)
```

```
z = x[:] # a copy not the same object
```

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- Write a function `middle(L)` which takes a list  $L$  as its argument, and returns the item in the middle position of  $L$ . (In order that the middle is well-defined, you should assume that  $L$  has odd length.) For example, calling `middle([8, 0, 100, 12, 1])` should return 100, since it is positioned exactly in the middle of the list. (`assert` is a useful tool to check assumptions — known as **preconditions** — are indeed true)
- Define a function `prod(L)` which returns the product of the elements in a list  $L$ . (for type hinting it is sometimes useful `from typing import Any`)

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- [https://classroom.github.com/a/gd\\_s1ybQ](https://classroom.github.com/a/gd_s1ybQ)
- <https://classroom.github.com/a/6AI0xnot>
- <https://classroom.github.com/a/exi-03Kl>



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# Lecture VI: Dictionaries, sets, comprehensions

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- Students: 27
- One triangle: tried by 22, 16 correct solutions
- Triangle kinds: tried by 20, 9 correct solutions
- DNA Hamming: tried by 19, 12 correct solutions
- Newton Sqrt: tried by 17, 13 correct solutions
- 7 students did all the exercises correctly

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# Dictionaries



A composite type `dict` that implements a **mapping** between immutable **keys** and **values**.

```
d = {'key': 'foo', 3: 'bar'}
```

```
print(d['key']) # 'foo'  
print(d[3])     # 'bar'  
print(d[2])     # error!
```

Notation is similar to lists/tuples, but **dicts** are not sequences indexed by numbers, you must use only the existing keys (`d.keys()`).

```
if x in d.keys():  
    print(d[x])
```

A sequence of values can be obtained with `d.values`. A sequence of 2-tuples (key, value) with `d.items()`.

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A **set** is a composite object with no duplicate (non mutable) elements. Common set operations are possible.

- Set literals: `{1,2,3}` `set()`
- `{1,2,3}.union({3,5,6})`  
`{1,2,3}.intersection({3,5,6})`

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# Comprehensions



**Comprehensions** are a concise way to create lists, sets, maps... It resembles the mathematical notation used for sets

$$A = \{a^2 | a \in \mathbb{N}\}.$$

```
squares = [x**2 for x in range(10)]
```

*# equivalent to:*

```
squares = []  
for x in range(10):  
    squares.append(x**2)
```

*# filtering is possible*

```
odds = [x for x in range(100) if x % 2 != 0]
```

*# with a set*

```
s = {x for x in range(50+1) if x % 5 == 0}
```

*# with a dict*

```
d = {x: x**2 for x in range(10)}
```

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A **file** is an abstraction the operating system uses to preserve data among the execution of programs. Data must be accessed **sequentially**.

- We need commands to ask to the OS to give access to a file (**open**).
- It is easy to read or write data **sequentially**, otherwise you need special commands (**seek**) to move the file “cursor”
- The number of open files is limited ( $\approx$  thousands), thus it is better to **close** files when they are not in use

Files contain bits (normally considered by group of bytes, 8 bits), the interpretation (“format”) is given by the programs which manipulate them. However, “lines of printable characters” (**plain text**) is a rather universal/predefined interpretation, normally the easiest to program.

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# File read access

```
f = open('filename.txt', 'r') # read only

# iterating on a file reads (all) the lines
for i in f:
    print(i)

# End of file already reached, result is ''
f.readline()

f.close()

# File closed, error!
f.readline()

To avoid remembering to close explicitly, Python provides the
context manager syntax.
with open('filename.txt', 'r') as f:
    for i in f:
        print(i)
```

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- Write a function to compute the complement of a DNA strand: every A becomes a T, every T an A, every C an G, every G an C.
- Apply the function to every line of a file with a DNA sequence
- Write a function that gives the set of (unique) sequences of 10 nucleic acids in a file

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- <https://classroom.github.com/a/MhchQHAd>
- <https://classroom.github.com/a/36ITXw1V>



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# Lecture VII: Procedural abstraction

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# Make a program readable



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You never write a program only for a machine! You, others, tools will *read* the program for different purposes. Every minute spent in making a program more understandable pays off hours saved later.

- **Type hinting** makes clear what a function needs to work properly, and what it produces
- **Documentation** helps understanding without the need to read implementation details
- **Examples of use** make easy to remember how to use a function and can be used for verification

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# Example

```
from typing import Union

Num = Union[int, float]

def cube(x: Num) -> Num:
    """Return the cube of x.

    >>> cube(-3)
    -27

    >>> abs(cube(0.2) - 0.008) < 10e-5
    True
    """
    return x * x * x
```

Examples can be tested by:  
`python -m doctest filename.py.`

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# Procedural abstraction

Procedural abstraction is key for our thinking process (remember the power of recursion, for example): giving a name to a procedure/function enhances our problem solving skills.

```
def sum_int(a: int, b: int) -> int:  
    """Sum integers from a through b.
```

```
>>> sum_int(1, 4)  
10
```

```
>>> sum_int(3, 3)  
3  
"""
```

```
assert b >= a  
result = 0  
for i in range(a, b+1):  
    result = result + i  
return result
```

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# Another “sum”



This is very similar...

```
def sum_cubes(a: int, b: int) -> int:
    """Sum the cubes of the integers from a through b.

    >>> sum_cubes(1, 3)
    36

    >>> sum_cubes(-2, 2)
    0

    """
    assert b >= a
    result = 0
    for i in range(a, b+1):
        result = result + int(cube(i))
    return result
```

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# Another “sum”



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This is also very similar...

$$\frac{1}{a \cdot (a+2)} + \frac{1}{(a+4) \cdot (a+6)} + \frac{1}{(a+8) \cdot (a+10)} + \dots + \frac{1}{(b-2) \cdot (b)}$$

(Leibniz:  $\frac{1}{1 \cdot 3} + \frac{1}{5 \cdot 7} + \frac{1}{9 \cdot 11} + \dots = \frac{\pi}{8}$ )



# Another “sum”



This is also very similar...

$$\frac{1}{a \cdot (a+2)} + \frac{1}{(a+4) \cdot (a+6)} + \frac{1}{(a+8) \cdot (a+10)} + \dots + \frac{1}{(b-2) \cdot (b)}$$

(Leibniz:  $\frac{1}{1 \cdot 3} + \frac{1}{5 \cdot 7} + \frac{1}{9 \cdot 11} + \dots = \frac{\pi}{8}$ )

```
def pi_sum(a: int, b: int) -> float:
    """Sum  $\frac{1}{a(a+2)}$  terms until  $(a+2) > b$ .

    >>> from math import pi
    >>> abs(8*pi_sum(1, 1001) - pi) < 10e-3
    True

    """
    assert b >= a
    result = 0.0
    for i in range(a, b+1, 4):
        result = result + (1 / (i * (i + 2)))
    return result
```

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# Can we abstract the similarity?



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```
from typing import Callable
```

```
def gen_sum(a: int, b: int, fun: Callable[[int], Num], step: int = 1) -> Num:  
    """Sum terms from a through b, incrementing by step.
```

```
>>> gen_sum(1, 4, lambda x: x)  
10
```

```
>>> gen_sum(1, 3, cube)  
36
```

```
>>> from math import pi  
>>> abs(8*gen_sum(1, 1000, lambda x: 1 / (x * (x + 2))), 4) - pi) < 10e-3  
True
```

```
"""
```

```
assert b >= a  
result = 0.0  
for i in range(a, b+1, step):  
    result = result + fun(i)  
if result.is_integer():  
    return int(result)  
return result
```

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- <https://classroom.github.com/a/5lBJ-wgC>



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# Lecture VIII: Object Oriented encapsulation

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# The huge value of procedural abstraction

It is worth to emphasize again the huge value brought by **procedural abstraction**. In Python it is not mandatory to use procedures/functions: the language is designed to be used also for *on the fly* calculations.

```
x = 45
s = 0
for i in range(0, x):
    s = s + i
```

This is ok, but it is not **encapsulated** (in fact, since encapsulation is so important you can at least consider it encapsulated in file which contains it)

- the piece of functionality is not easily to distinguish

it could be intertwined with other unrelated code

```
x = 45
a = 67 # another concern
s = 0
for i in range(0, x):
    s = s + i
print(a) # another concern
```

- the goal is not explicit, which data are needed, what computes
- it's hard to reuse even in slightly different contexts

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# Encapsulate the functionality

```
def sum_to(x: int) -> int:
    assert x >= 0
    r = 0
    for i in range(0, x):
        r = r + i
    return r
```

```
s = sum_to(45)
```

- It gives to our mind a “piece of functionality”, the interpreter we are programming is now “able” to do a new thing that can be used **without thinking about the internal details**
- It makes clear which data it needs (an integer,  $\geq 0$  if we add also an assertion or a docstring)
- It makes clear that the interesting result is another integer produced by the calculation
- It can be reused easily and safely



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# Object Oriented encapsulation



Encapsulation is so important that it is used also at a higher level: a collection of related procedures.

```
x = 666
```

```
def increment():
```

```
    x = x + 1
```

```
def decrement():
```

```
    x = x - 1
```

Again: this is correct Python code, but it has problems:

- Both the functions depends on `x` but this is not clear from their **signature**: a user must look at the internal details
- The two functions cannot be reused individually, but only together with the other (and `x`)

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# Classes

A **class** is a way to package together a collection of related functions. The class is a “mold” to instance new **objects** that encapsulated the related functionalities.

```
class Counter:
    def __init__(self, start: int):
        self.x = start

    def increment(self):
        self.x = self.x + 1

    def decrement(self):
        self.x = self.x - 1
```

```
c = Counter(666)
c.decrement()
d = Counter(999)
d.increment()
```

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- <https://classroom.github.com/a/JMlHieUy>
- Optional: GitHub has a new assignment on git and GitHub basics; try it here  
<https://classroom.github.com/a/KLoZ8Qxl>



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# Lecture IX: Random numbers

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# Exercise



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Write a Python program which chooses an integer 1–10 and asks to the user to guess it

- if the number given by the user is not 1–10, it prints “Invalid”;
- if the number is the chosen one, it prints “Yes!”;
- otherwise “You didn’t guess it...”.

Evolve the program for asking until the user guess the number correctly giving hints (“higher...”, “lower...”).

```
from random import randint
```

```
# To get a random integer in the set [1..10]  
randint(1, 10)
```

# Random numbers



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**Pseudorandomness:** the sequence of numbers is not predictable...

```
from random import randint
```

```
for _ in range(0,10):  
    print randint(1, 100)
```

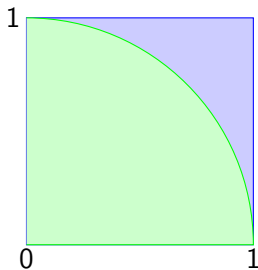
unless you know the **seed**.

```
from random import seed, randint
```

```
seed(292)  
for _ in range(0,10):  
    print randint(1, 100)
```



# Example



- Blue square: 1
- Green area:  $\frac{\pi}{4}$

The **Monte Carlo** method consists of choosing sample experiments at random from a large set and then making deductions on the basis of the probabilities estimated from frequency of occurrences.

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# Example



```
from random import random

def approx_pi(tries: int) -> float:
    """Return an approximation for pi.

    >>> from math import pi
    >>> from random import seed
    >>> seed(7897) # Tests should be reproducible
    >>> abs(4*approx_pi(1000) - pi) < 10e-2
    True

    >>> abs(4*approx_pi(100000) - pi) < abs(approx_pi(1000) - pi)
    True
    """

    within_circle = 0
    for i in range(0, tries):
        x = random() # range [0,1)
        y = random()
        if (x**2+y**2)**0.5 < 1:
            within_circle += 1
    return within_circle / tries
```

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# Example

It's easy to extend to make this work for any function on  $[0, 1)$ .

```
from random import random
from typing import Callable

def approx_fun(predicate: Callable[[float, float], bool], tries:
↳ int) -> float:
    """Return an approximation for pi.

    >>> from math import pi
    >>> from random import seed
    >>> seed(7897) # Tests should be reproducible
    >>> within_circle = lambda x, y: x**2 + y**2 < 1
    >>> abs(4*approx_fun(within_circle, 1000) - pi) < 10e-2
    True
    """

    true_cases = 0
    for i in range(0, tries):
        x = random() # range [0,1)
        y = random()
        if predicate(x, y):
            true_cases += 1
    return true_cases / tries
```

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# Simulations



Random number are useful also for *simulation*: for example, we could simulate **evolutionary drift**.

```
from random import seed, randint

class DriftSimulation:
    def __init__(self, sim_seed: int = 232943):
        self.population = ['\N{MONKEY}', '\N{TIGER}', '\N{BUTTERFLY}', '\N{LIZARD}',
                           ↪ '\N{SNAIL}']
        seed(sim_seed)

    def offspring(self):
        new = self.population[randint(0, len(self.population)-1)]
        self.population[randint(0, len(self.population)-1)] = new

    def simulate(self, generations: int):
        for i in range(0, generations):
            self.offspring()

s = DriftSimulation()
for i in range(100):
    line = str(i)
    for a in s.population:
        line = line + ' ' + a
    print(line)
    if len(set(s.population)) == 1:
        break
s.simulate(1)
```

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# Lecture X: Using Third-party libraries

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# Third-party libraries



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Python is “sold” *batteries included* (with many useful built-in libraries). Moreover, like many modern programming environments, it has standard **online package directories** that list libraries produced by independent developers.

<https://pypi.org/>

The Python package index currently lists almost 300K libraries!

# Installing a library



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The details are explained here: <https://packaging.python.org/tutorials/installing-packages/>

- In most cases it is very easy, the pip program does all the magic
- It is **very** important to understand the difference between a **system-wide** and a **project-specific** installation.

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# System-wide vs. Project-specific



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If you don't take special precautions, a package is installed in a way that makes it available to your Python system: every Python interpreter you launch sees them.

- In many cases, this is **not** what you want
- **Different projects/programs might depend on different versions of the libraries**
- Libraries themselves depend on other libraries, you want to understand exactly which packages your program is using in order to **reproduce** the settings on other machines

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Python provides the idea of **virtual development environments** (venv)

- You can create one with: `python -m venv CHOOSE_A_NAME`
- You must activate it (syntax depends on your OS):  
`CHOOSE_A_NAME\Scripts \activate`
- In an active virtual environment all the installation are **confined** to it
- You can get the list of installed packages with `pip freeze`

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# Simplified venv administration



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Virtual environments are key to avoid messing up your system.  
Many tools simplify their administration.

- `pipenv` (my preferred one, we will use this)
- `poetry` (similar to `pipenv`, currently less popular, but it has a better dependency control, a bit more complex)
- `conda` (uses its own package index, great flexibility and complexity, manage different python versions)

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# Virtual environments caveats



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When you are working in a Python virtual environment, remember to launch **all** your development tools “inside” the virtual space.

For example, to use IDLE don't click on the main application launcher, instead: `python -m idlelib`.

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NumPy is a third-party library very popular for scientific/numerical programming (<https://numpy.org/>).

- Features familiar to `matlab`, R, Julia programmers
- The key data structure is the `array`
  - 1-dimension arrays: `vectors`
  - 2-dimension arrays: `matrices`
  - n-dimension arrays

In some languages array is more or less synonym of list: Python distinguishes: `lists` (mutable, arbitrary elements), `arrays` (mutable, all elements have the same type), `tuples` (immutable, fixed length, arbitrary elements).



# State of the homework



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- One-triangle: tried by 26, ok for 18
- triangle-kinds: tried by 22, ok for 11
- dna-hamming: tried by 22, ok for 14
- newton-sqrt: tried by 21, ok for 15
- py-triplets: tried by 19, ok for 13
- flatten-list: tried by 19, ok for 6
- dna-files: tried by 20, ok for 7
- dna-forensics: tried by 14, ok for 5

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# Lecture XI: NumPy arrays

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# NumPy arrays



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The most important data structure in NumPy is `ndarray`: a (usually fixed-size) sequence of same type elements, organized in one or more dimensions.

<https://numpy.org/doc/stable/reference/arrays.ndarray.html>

Implementation is based on byte arrays: accessing an element (all of the same byte-size) is virtually just the computation of an 'address'.

# Why?



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- using NumPy arrays is often more compact, especially when there's more than one dimension
- faster than lists when the operation can be **vectorized**
- (slower than lists when you append elements to the end)
- can be used with element of different types but this is less efficient

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A ndarray has a dtype (the type of elements) and a shape (the length of the array on each dimensional **axis**). (Note the jargon: slightly different from linear algebra)

- Since appending is costly, normally they are pre-allocated (zeros, ones, arange, linspace, ...)
- vectorized operations can simplify code (no need for loops) and they are faster with big arrays
- vector indexing syntax (similar to R): very convenient (but you need to learn something new)

# All the elements must have the same size



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This is actually a big limitation: the faster access comes with a price in flexibility.

```
>>> np.array(['', '', ''])
array(['', '', ''], dtype='<U1')
>>> np.array(['a', 'bb', 'ccc'])
array(['a', 'bb', 'ccc'], dtype='<U3')
>>> np.array(['a', 'bb', 'cccccccccccccccccccccccc'])
array(['a', 'bb', 'cccccccccccccccccccccccc'], dtype='<U21')
```

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# Usually the length is not changed

The best use of arrays is to avoid a change in their length, that can be costly. Thus, they are normally **preallocated** at creation:

- `np.array([1,2,3])`
- `np.zeros(2)`, `np.zeros(2, float)`, `np.ones(2)`
- `np.empty((2,3))` six not meaningful float values
- `np.arange(1, 5)` be careful with floats:  

```
>>> np.arange(0.4, 0.8, 0.1)
array([0.4, 0.5, 0.6, 0.7])
>>> np.arange(0.5, 0.8, 0.1)
array([0.5, 0.6, 0.7, 0.8])
```
- `np.linspace(0.5, 0.8, 3)` with this the length is easier to predict

You can concatenate arrays with `np.concatenate` (be careful with the shapes!)

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# Don't remove, select

In general you don't remove elements but select them. Be careful: if you don't make an explicit **copy** you get a "view" and possibly side-effects.

```
>>> a = np.ones((2,3))
>>> a
array([[1., 1., 1.],
       [1., 1., 1.]])
>>> x = a[:, 1]
>>> x
array([1., 1.])
>>> x[0] = 0
>>> x
array([0., 1.])
>>> a
array([[1., 0., 1.],
       [1., 1., 1.]])
```

```
>>> x = a[:, 1].copy()
>>> x[1] = 100
>>> x
array([ 0., 100.])
>>> a
array([[1., 0., 1.],
       [1., 1., 1.]])
```

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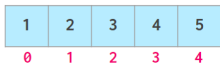
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# Indexing is powerful

```
a = np.arange(1, 6)
```



`a[1]`



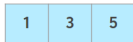
`a[2:4]`



`a[-2:]`



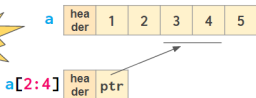
`a[::2]`



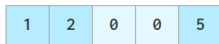
`a[[1,3,4]]`



"fancy indexing"



`a[2:4] = 0`



Picture from "NumPy Illustrated: The Visual Guide to NumPy", highly recommended

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# Indexing is powerful

a	1	2	3	4	5	6	7	6	5	4	3	2	1
---	---	---	---	---	---	---	---	---	---	---	---	---	---

a > 5	False	False	False	False	False	True	True	True	False	False	False	False	False
-------	-------	-------	-------	-------	-------	------	------	------	-------	-------	-------	-------	-------

`np.any(a > 5)`

True

`a[a > 5]`

6	7	6
---	---	---

`np.all(a > 5)`

False

`a[a > 5] = 0`

a	1	2	3	4	5	0	0	0	5	4	3	2	1
---	---	---	---	---	---	---	---	---	---	---	---	---	---

`a[(a >= 3) & (a <= 5)] = 0`

a	1	2	0	0	0	6	7	6	0	0	0	2	1
---	---	---	---	---	---	---	---	---	---	---	---	---	---

&	and
	or
^	xor
~	not

Picture from "NumPy Illustrated: The Visual Guide to NumPy", highly recommended

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# The highest power: vectorization



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Most of the basic mathematical function are **vectorized**: no need for loops! This is both convenient and faster!

```
>>> a = np.array([1,2,3,4])
>>> a + 1
array([2, 3, 4, 5])
>>> a ** 2
array([ 1,  4,  9, 16])
>>> np.exp(a)
array([ 2.71828183,  7.3890561 , 20.08553692,
        ↪ 54.59815003])
```

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# Array operations



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On arrays you have many “aggregate” operations.

```
>>> a
array([1, 2, 3, 4])
>>> a.sum()
10
>>> a.max()
4
>>> a.argmin()
0
>>> a.mean()
2.5
```

Remember to look at `dir` or the online documentation.

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<https://classroom.github.com/a/C0132nII>



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# Lecture XII: Matplotlib

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# Matplotlib



When you have arrays with many data it is useful to have a way to display them graphically.

- The most popular is `matplotlib`  
<https://matplotlib.org/>
- Many other graphical frameworks (e.g., `seaborn`) based on it
- Many, many possibilities to tune your graphics! It's hard to master every detail.
- Be careful: it can be used with two different styles.
  - 1 The (preferred) object-oriented way: clean and rational, but a bit more verbose
  - 2 The procedural way: mostly useful only for “throw-away” scripts, but for this reason more common in the examples you can find online

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# Graphical output is an operating system service



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- Output is a service provided by the operating system: *textual* output is very standardized even across different platform, **graphics is not so stable**
- When you deal with graphical programs: expect installation headaches, portability glitches, etc.

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# A real world example



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On the Win10 platform where I try the programs:

- the current `matplotlib` library doesn't work: it installs, but when used it complains about missing DLLs (Dynamic libraries shared among the programs)
- according to the "Internet" ... the problem can be solved by installing Visual Studio (!): I didn't try...
- The last version I found working properly is 3.3.1: I will stick to that (thanks to the virtual environments this is not a problem)
- On other platforms (Linux, Mac): no problems, but better if we use all the same version

BTW, it depends on `numpy`

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# The OO style



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- You need always to objects: a Figure and a Axes
- plotting happens on axes, framed in a figure
- very flexible: you can add plots on the same axis, or you can have many axes collected in a single figure

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# Basic example



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```
import numpy as np
import matplotlib.pyplot as plt

x = np.linspace(-2*np.pi, 2*np.pi, 100)

fig, ax = plt.subplots()

ax.plot(x, np.sin(x))

fig.show()
```

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# Many different types of charts



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If `ax` is a `Axes`

- Scatter-plots `ax.scatter`
- Bar-plots `ax.bar`
- Histograms `ax.hist`
- 2D `ax.imshow`

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- add labels, legends, titles
- add a grid
- combine multiple plots on the same axis
- combine multiple axes on the same figure

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# Save your pictures!



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A `Figure` can be saved in a file with `savefig`. You should keep in mind the difference between:

- bitmap formats (`png` `jpg` ...): the file is matrix of pixels
- vector formats (`svg` `pdf` ...): the file is a set of instructions to reproduce the picture, less portable but it can be magnified

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# Lecture XIII: A game of life

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# A game of life



In 1970, J.H. Conway proposed his **Game of Life**, a simulation on a 2D grid:

- 1 Every cell can be *alive* or *dead*: the game start with a population of alive cells (*seed*)
- 2 any alive cell with less of 2 alive neighbours dies (*underpopulation*)
- 3 any alive cell with more than 3 alive neighbours dies (*overpopulation*)
- 4 any dead cell with exactly 3 alive neighbours becomes alive (*reproduction*)

The game is surprisingly rich: many mathematicians, computer scientists, biologists. . . spent their careers on the emerging patterns!

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# Life forms



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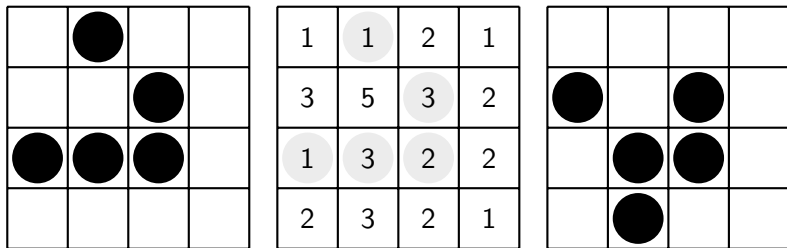
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There are names for many “life forms”: *still lifes*, *oscillators*, *starships*...

A famous starship is the **glider**:



The glider repeats itself in another position after 4 generations.

# Python implementation



To implement a Game of Life simulation in Python, we can:

- use a ndarray for the grid
- each cell contains 0 (dead) or 1 (alive)
- for simplicity we can add a “border” of zeros

0	0	0	0	0
0	1	1	1	0
0	1	0	1	0
0	1	1	0	0
0	0	0	0	0

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# Avoid loops

For a 1-D array X

0	1	1	0	1	0
---	---	---	---	---	---

All the neighbours on the right  $X[2:]$

0	1	1	0	1	0
---	---	---	---	---	---

All the neighbours on the left  $X[:-2]$

What does  $X[2:] + X[:-2]$  represent? The sum is (yellow) element by (yellow) element, the result is:  $[1, 1, 2, 0]$

Can you think to a similar solution for the 2-D case?

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# Avoid loops



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0	0	0	0	0	0
0	<b>0</b>	<b>1</b>	<b>0</b>	<b>0</b>	<b>0</b>
0	<b>0</b>	<b>0</b>	<b>1</b>	<b>0</b>	<b>0</b>
0	<b>1</b>	<b>1</b>	<b>1</b>	<b>0</b>	<b>0</b>
0	<b>0</b>	<b>0</b>	<b>0</b>	<b>0</b>	<b>0</b>
0	0	0	0	0	0

```
X[1:-1, 2:]
```

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# Avoid loops



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0	0	0	0	0	0
0	<b>0</b>	<b>1</b>	<b>0</b>	<b>0</b>	<b>0</b>
0	<b>0</b>	<b>0</b>	<b>1</b>	<b>0</b>	<b>0</b>
0	<b>1</b>	<b>1</b>	<b>1</b>	<b>0</b>	<b>0</b>
0	<b>0</b>	<b>0</b>	<b>0</b>	<b>0</b>	<b>0</b>
0	0	0	0	0	0

`X[2:,2:]`

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# Avoid loops



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0	0	0	0	0	0
0	<b>0</b>	<b>1</b>	<b>0</b>	<b>0</b>	0
0	<b>0</b>	<b>0</b>	<b>1</b>	<b>0</b>	0
0	<b>1</b>	<b>1</b>	<b>1</b>	<b>0</b>	0
0	<b>0</b>	<b>0</b>	<b>0</b>	<b>0</b>	0
0	<b>0</b>	<b>0</b>	<b>0</b>	<b>0</b>	0

`X[2: , 1:-1]`

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# Avoid loops



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0	0	0	0	0	0
0	<b>0</b>	<b>1</b>	<b>0</b>	<b>0</b>	0
0	<b>0</b>	<b>0</b>	<b>1</b>	<b>0</b>	0
0	<b>1</b>	<b>1</b>	<b>1</b>	<b>0</b>	0
0	<b>0</b>	<b>0</b>	<b>0</b>	<b>0</b>	0
0	<b>0</b>	<b>0</b>	<b>0</b>	<b>0</b>	0

$X[2:, 1:-1]$

And other 5 matrices...

# Avoid loops



						X
0	0	0	0	0	0	
0	0	1	0	0	0	
0	0	0	1	0	0	
0	1	1	1	0	0	
0	0	0	0	0	0	
0	0	0	0	0	0	

$$X == 1$$

						N
0	0	0	0	0	0	
0	1	1	2	1	0	
0	3	5	3	2	0	
0	1	3	2	2	0	
0	2	3	2	1	0	
0	0	0	0	0	0	

$$N > 3$$

Death by overpopulation:  $X[(X == 1) \& (N > 3)] = 0$   
(empty in this case!)

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# Lecture XIV: Laplacian operator

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# Gray-Scott systems



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Systems driven by the Gray-Scott equation exhibit Turing patterns ( $D_u, D_v, f, k$  are constants).

$$\frac{\partial u}{\partial t} = D_u \nabla^2 u - uv^2 + f \cdot (1 - u)$$
$$\frac{\partial v}{\partial t} = D_v \nabla^2 v + uv^2 - (f + k) \cdot v$$

- These give the **change** of  $u$  and  $v$  over time
- The diffusion term can be approximated on a grid by computing the discrete Laplacian

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# Discrete Laplacian



$$\nabla^2 = \nabla \cdot \nabla = \frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2}$$

- Change on a grid (1-D):

$$\nabla f[n] = f[n+1] - f[n]$$

$$\nabla f[n] = f[n] - f[n-1]$$

- Second order change (1-D):

$$\begin{aligned}\nabla(\nabla f[n]) &= \nabla(f[n+1] - f[n]) \\ &= (f[n+1] - f[n]) - (f[n] - f[n-1]) \\ &= f[n-1] - 2f[n] + f[n+1]\end{aligned}$$

- In 2-D we do this independently on the 2 dimensions  $n, m$ :

$$\begin{aligned}\nabla(\nabla f[n, m]) &= f[n-1, m] - 2f[n, m] + f[n+1, m] + \\ &\quad f[n, m-1] - 2f[n, m] + f[n, m+1] \\ &= f[n-1, m] + f[n+1, m] + f[n, m-1] + f[n, m+1] - 4f[n, m]\end{aligned}$$

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# Vectorization



0	0	0	0	0	0
0	13	14	15	16	0
0	9	10	11	12	0
0	5	6	7	8	0
0	1	2	3	4	0
0	0	0	0	0	0

`X[1:-1, 2:]`

Ignoring the border, the right neighbour of  $(i, j)$  is  $(i, j + 1)$  in the inner white and  $(i, j)$  in the yellow: in the inner white 11 is  $(1, 3)$ , its neighbour 12 is  $(1, 4)$ , but  $(1, 3)$  in the yellow.

This way one can compute the Laplacian matrix using only vectorized plus.

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# Lecture XV: Tabular data

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# Tabular data



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Data are often given/collected as **tables**: matrices with rows for individual records and columns for the fields of the records. This is especially common in statistics, R has a built-in type for this: the **dataframe**.

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pandas (Python for data analysis) brings the DataFrame type to Python. It is based on numpy.

- **Series**: a one-dimensional labeled array capable of holding any data type (integers, strings, floating point numbers, Python objects, etc.). The axis labels are collectively referred to as the **index**.
- **DataFrame**: a 2-dimensional labeled data structure with columns of potentially different types. You can think of it like a spreadsheet, or a **dict** of Series objects.



```
import pandas as pd
```

```
s = pd.Series(np.random.randn(5), index=["a", "b",  
    ↪ "c", "d", "e"])
```

s is a numpy array of floats, each one has a label.

```
d = {"b": 1, "a": 0, "c": 2}
```

```
s = pd.Series(d)
```

The ordering depends on Python and pandas version... The current ones takes the insertion order, but you can provide explicitly the index.

```
d = {"b": 1, "a": 0, "c": 2}
```

```
s = pd.Series(d, index=['a', 'b', 'c'])
```





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A Series is convenient because it is a ndarray (and can be vectorized) but also a dict.

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# Dataframes



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```
d = { "one": pd.Series([1.0, 2.0, 3.0], index=["a",  
↪ "b", "c"]),  
      "two": pd.Series([1.0, 2.0, 3.0, 4.0],  
↪ index=["a", "b", "c", "d"]),  
    }
```

```
df = pd.DataFrame(d)
```

A DataFrame has an `index` and a `columns` attribute.  
There are many ways of creating DataFrames, see the docs.

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# From csv or spreadsheets



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A famous example: Fisher's Iris flowers dataset.  
150 records, "sepal length", "sepal width", "petal length", "petal width", "class"  
`iris = pd.read_csv('iris.csv')`

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# Two ways of indexing



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- `.loc[]` “label based”
- `.iloc[]` “position based”

For both you can use: a single value, a list of values, a boolean array. Two notable things:

- 1 If you use a slice notation with `.loc ('a': 'f')` the last value is included! (different from plain python and from `.iloc`)
- 2 Can be also a callable function with one argument (the calling Series or DataFrame) and that returns valid output for indexing (one of the above)

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# Lecture XVI: Inheritance

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# Destructuring a bound computation



```
def approx_euler(t: np.ndarray, f0: float, dfun:
↳ Callable[[float], float]) -> np.ndarray:
    """Compute the Euler approximation of a function on
↳ times t, with derivative dfun.
    """
    res = np.zeros_like(t)
    res[0] = f0

    for i in range(1, len(t)):
        res[i] = res[i-1] + (t[i]-t[i-1])*dfun(res[i-1])

    return res
```

Since we approximate the solution of a differential equation  $p' = f(p, t)$ , we used the trick of writing `dfun` as a function of `p`: this is why we call it by passing a point of `res` (and not of `pyt`). This trick makes it possible to compute it *together* with `res` itself (given the initial condition).

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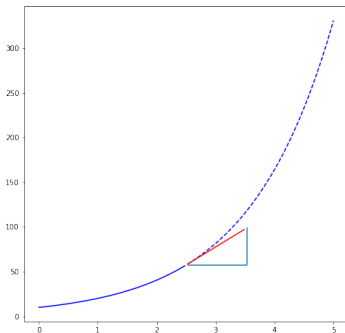
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# Two things together

A good way to keep two things **separate** (thus they can be changed independently), but **together** is the object-oriented approach: a **class** is a *small world* in which several computations are bound together, they share data and can depend one on each other.



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# OOP approach



```
class EulerSolver:
```

```
    """An EulerSolver object computes the Euler approximation of a differential equation  
    ↪  $p' = f(p, t)$ ."""
```

```
    Create it by giving the  $f$  function, then set the initial condition  $P_0$ .  
    The approximate solution on a given time span is computed by the method solve.  
    """
```

```
def __init__(self, f: Callable[[float, float], float], float):  
    self.f = f
```

```
def set_initial_condition(self, P0: float):  
    self.P0 = P0
```

```
def solve(self, time: np.ndarray) -> np.ndarray:  
    """Compute  $p$  for  $t$  values over time."""  
    self.t = time  
    self.p = np.zeros_like(self.t)  
    # ....
```

```
def _diff(self, i: int) -> float:  
    """Compute the differential increment at time of index  $i$ ."""  
  
    assert i >= 0  
    # ...
```

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# How to use it



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```
time = np.linspace(0, 5, 100)
```

```
solver = EulerSolver(lambda p, t: 0.7*p)
```

```
solver.set_initial_condition(10)
```

```
euler = solver.solve(time)
```

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# What we have gained



Conceptual steps are separated (but kept together by the class). We can decide to change one of them independently. Object-oriented programming has a feature to make this easy:

## inheritance

```
class RKSolver(EulerSolver):
    def _diff(self, i: int) -> float:
        """Compute the differential increment at time
        ↪ of index i."""

        assert i >= 0
        # use Runge-Kutta now!
        # overridden functionality is available with
        # super()._diff(i)
```

RKSolver **inherits** the methods of EulerSolver and it **overrides** the method `_diff`.

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# Substitution principle



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If inheritance is done properly (unfortunately not trivial in many cases), the new class can be used wherever the old one was.

```
solver = RKSolver(lambda p, t: 0.7*p)
solver.set_initial_condition(10)
rk = solver.solve(time)
```

Overridden methods must be executable when the old ones were and their must produce at least the “same effects” (Liskov’s principle).

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# Lecture XVII: Exception handling, Iterators

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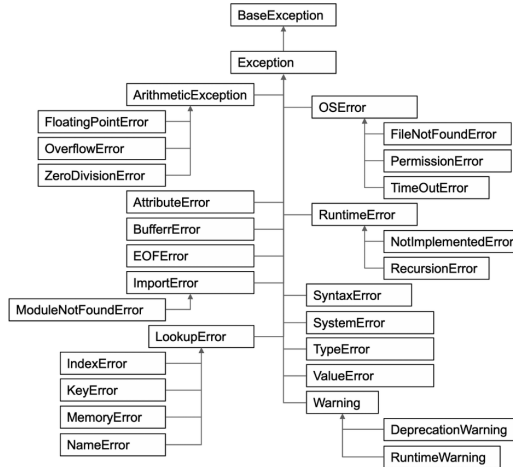
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# Exceptions



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- **Exceptions** and **Errors** are object **raised** (or thrown) in the middle of an anomalous computation.
- Exceptions change the control flow: the control passes to the “closer” **handler**, if it exists: otherwise it **aborts**.



# Exception handling



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Exceptions can be **handled**: the strategy is normally an “organized panic” in which the programmer tidies up the environment and exits.

```
danger()  
# An exception in danger  
# aborts the program
```

```
try:  
    danger()  
except:  
    # An exception in danger  
    # it's handled here
```

```
try:  
    danger()  
except OverflowError as e:  
    # An exception in danger  
    # it's handled here  
    # The object is referred  
    ↪ by e  
finally:  
    # This is executed in any  
    ↪ case
```

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# Raising an exception



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To explicitly raise an exception, use the `raise` statement

```
if something == WRONG:  
    raise ValueError(f'The value {something} is wrong!')
```

Assertions are a disciplined way to raise exceptions.



Object can be **iterable**. Python defines the iterator protocol as:

- `iterator.__iter__()` Return the iterator object itself. This is required to allow both containers and iterators to be used with the `for` and `in` statements.
- `iterator.__next__()` Return the next item from the container. If there are no further items, raise the `StopIteration` exception.



# Notable iterators



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Built-in lists, tuples, ranges, sets, dicts are iterators.

- Numpy arrays
- Pandas Series and DataFrames

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# Pandas DataFrame



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Be careful: the default iteration is on **column names** (similar to dicts, which iterate on keys).

- `iterrows()`: Iterate over the rows of a DataFrame as (index, Series) pairs. This converts the rows to Series objects, which can change the dtypes and has some performance implications.
- `itertuples()`: Iterate over the rows of a DataFrame as namedtuples of the values. This is a lot faster than `iterrows()`, and is in most cases preferable to use to iterate over the values of a DataFrame.

Iterating is **slow**: whenever possible try to use vectorized operation or **function application**.

# Pandas function application



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```
# apply the function to each column  
df.apply(lambda col: col.mean() + 3)
```

```
# apply the function to each row  
df.apply(lambda row: row + 3, axis=1)
```

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# Pandas query



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```
df[df['A A'] > 3]
```

*# equivalent to this (backticks because of the space)*

```
df.query('`A A` > 3')
```

*# query can also refer to the index*

```
df.query('index >= 15')
```

*# same as*

```
df[15:]
```

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# Lecture XVIII: Probabilistic programming

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# How science works



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Describing one single “scientific method” is problematic, but a schema many will accept is:

- 1 Imagine a **hypothesis**
- 2 Design (mathematical/convenient) **models** consistent with the hypothesis
- 3 Collect experimental **data**
- 4 Discuss the fitness of data given the models

It is worth noting that the falsification of models is not *automatically* a rejection of hypotheses (and, more obviously, neither a validation).

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# The role of Bayes Theorem



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In this discussion, a useful relationship between data and models is Bayes Theorem.

$$P(M, D) = P(M|D) \cdot P(D) = P(D|M) \cdot P(M)$$

Therefore:

$$P(M|D) = \frac{P(D|M) \cdot P(M)}{P(D)}$$

The plausibility of the model given some observed data, is proportional to the number of ways data can be *produced* by the model and the prior plausibility of the model itself.

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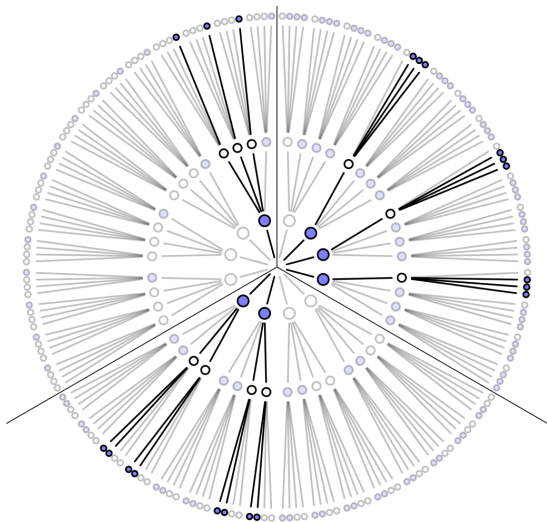
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# Simple example



- Model: a bag with 4 balls in 2 colors
- Observed: BWB
- Which is the plausibility of BBBB, BBBW, BBWW, BWWW, WWWW?

Bayes Theorem is the formalization of this **counting**



Picture from: R. McElreath, Statistical Rethinking

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# A computational approach



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This Bayesian strategy is (conceptually) easy to transform in a computational process.

- 1 Code the models
- 2 Run the models
- 3 Compute the plausibility of the models based on observed data

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# Classical binomial example



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- Which is the proportion  $p$  of water covering Earth? The models are indexed by the float  $0 < p < 1$
- Given  $p$ , the probability of observing some  $W, L$  in a series of **independent random observations** is:  
$$P(W, L|p) = \frac{(W+L)!}{W! \cdot L!} p^W \cdot (1-p)^L$$
 (binomial distribution).
- Do we have an initial (prior) idea?
- Make observations, apply Bayes, update prior!

# A conventional way of expressing the model



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$$W \sim \text{Binomial}(W + L, p)$$

$$p \sim \text{Uniform}(0, 1)$$

**Probabilistic programming** is systematic way of coding this kind of models, combining predefined statistical distributions and Monte Carlo methods for computing the posterior plausibility of parameters.

# In principle you can do it by hand



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```
def dbinom(success: int, size: int, prob: float) -> float:
    fail = size - success
    return np.math.factorial(size)/(np.math.factorial(success)*np.math.factorial(fail))*p ]
    ↪ rob**success*(1-prob)**(fail)

W, L = 7, 3
p_grid = np.linspace(start=0, stop=1, num=20)
prior = np.array([1] * 20)

likelihood = dbinom(W, n=W+L, p=p_grid)

unstd_posterior = likelihood * prior

posterior = unstd_posterior / unstd_posterior.sum()
```

Unfeasible with many variables!

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```
import pymc as pm
```

```
W, L = 7, 3
```

```
earth = pm.Model()
```

```
with earth:
```

```
    p = pm.Uniform("p", 0, 1) # uniform prior
```

```
    w = pm.Binomial("w", n=W+L, p=p, observed=W)
```

```
    posterior = pm.sample(2000)
```

```
posterior['p']
```

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# Lecture XIX: Behind pymc3

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The probabilistic programming approach of `pymc3` is built on two “technologies”:

- 1 A library that mixes numerical and symbolic computations (Theano, soon becoming Aesara)
- 2 Markov Chain Monte-Carlo (MCMC) algorithms to estimate posterior densities

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It bounds numerical computations to its symbolic structure  
("graph")

```
import theano
from theano import tensor

a = tensor.dscalar('alpha')
b = tensor.dscalar('beta')

c = a + b**2

f = theano.function([a,b], c)

assert f(1.5, 2) == 5.5
```



# Symbolic manipulations



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Variables can be used to compute values, but also symbolic manipulations.

```
d = tensor.grad(c, b)
```

```
f_prime = theano.function([a, b], d)
```

```
assert f_prime(1.5, 2) == 4.
```

Note you still need to give an a because the symbolic structure needs it.

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It's way of estimating (relative) populations of “contiguous” states.

- It needs the capacity of evaluate the population/magnitude of any two close states (but a global knowledge of all the states *at the same time*)
- It's useful to estimate *posterior* distribution *without explicitly computing*  $P(D)$ : 
$$P(M|D) = \frac{P(D|M) \cdot P(M)}{P(D)}$$

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# Metropolis



The easiest MCMC approach is the so-called **Metropolis** algorithm (in fact appeared as Metropolis, N., **Rosenbluth, A., Rosenbluth, M.**, Teller, A., and Teller, E., 1953)

```
steps = 100000
positions = np.zeros(steps)
populations = [1,2,3,4,5,6,7,8,9,10]
current = 3

for i in range(steps):
    positions[i] = current
    proposal = (current + np.random.choice([-1,1])) %
        ↪ len(populations)
    prob_move = populations[proposal] /
        ↪ populations[current]
    if np.random.uniform(0, 1) < prob_move:
        current = proposal
```

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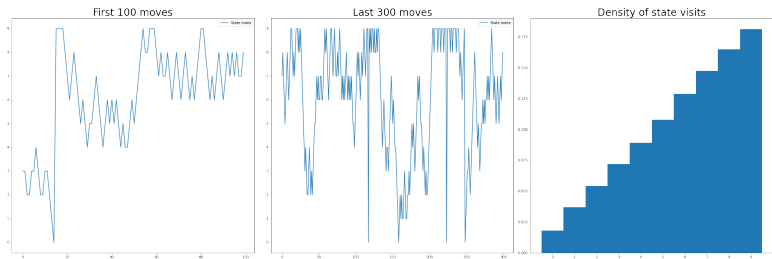
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# Convergence



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**Eventual** convergence is guaranteed, but it can be painful slow (and you don't know if you are there... ). Many algorithms try to improve: Gibbs, Hamiltonian-MC, NUTS...

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# Putting them together



```
import pymc3 as pm

linear_regression = pm.Model()

with linear_regression:
    # Theano variables
    sigma = pm.Uniform('sigma_h', 0, 50)
    alpha = pm.Normal('alpha', 178, 20)
    beta = pm.Normal('beta', 0, 10)
    mu = alpha + beta*(adult_males['weight'] -
    ↪ adult_males['weight'].mean())
    # Observed!
    h = pm.Normal('height', mu, sigma,
    ↪ observed=adult_males['height'])

trace = pm.sample() # MCMC sampling
```

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