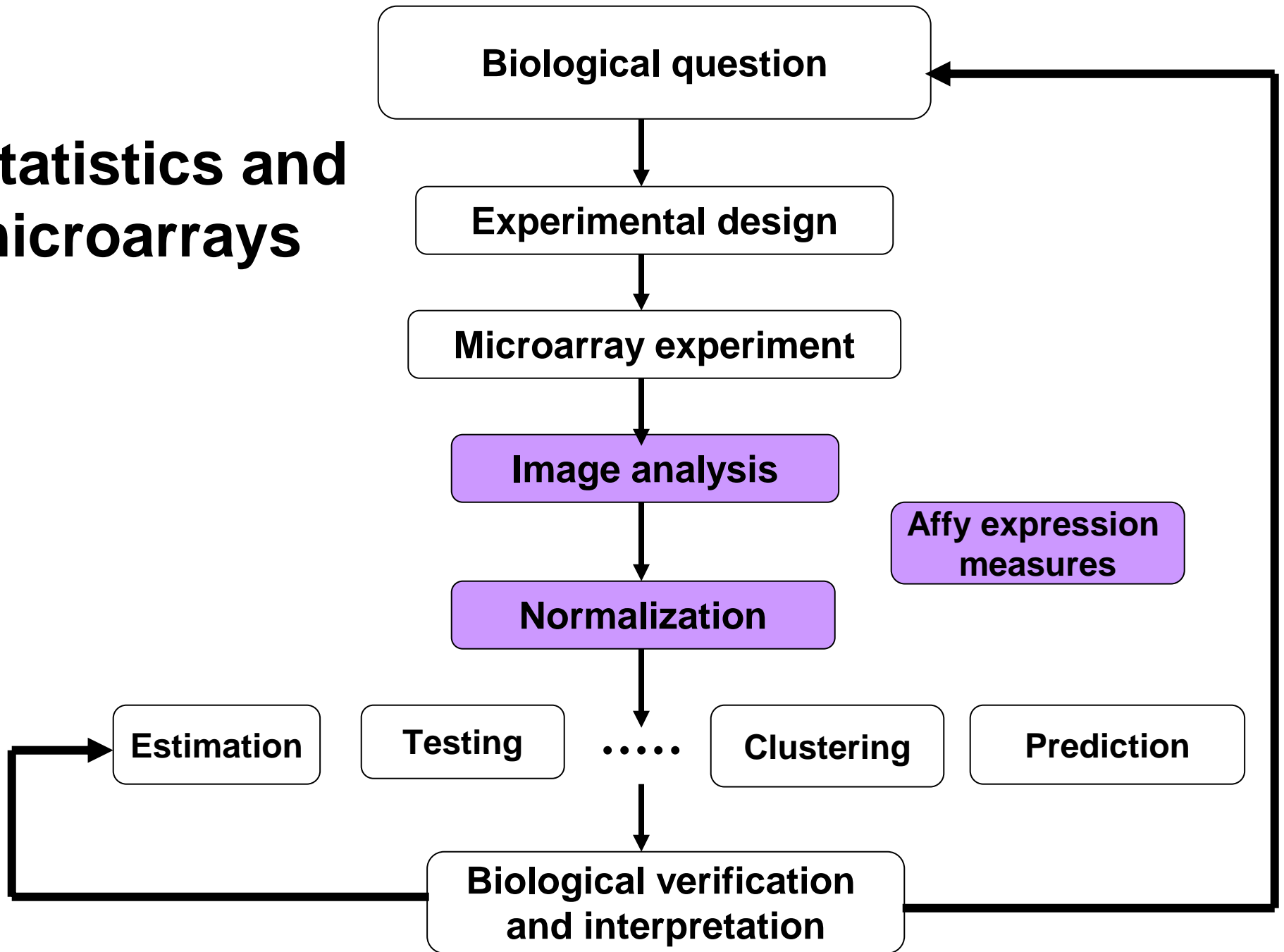


# **Pre-processing in cDNA microarray experiments**

**Sandrine Dudoit, Robert Gentleman,  
Rafael Irizarry, and Yee Hwa Yang**

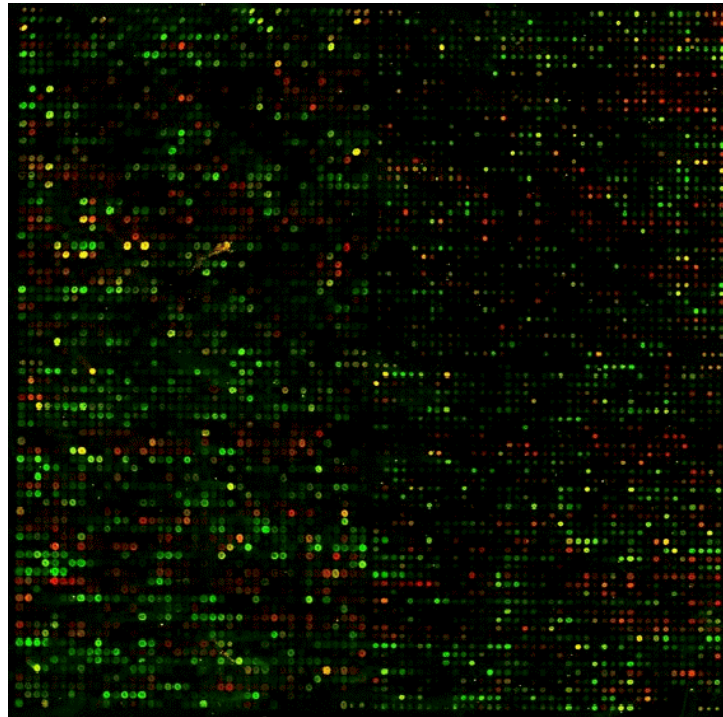
# Statistics and microarrays



# Outline

- cDNA microarrays
  - Image analysis;
  - Normalization.
- Affymetrix oligonucleotide chips
  - Image analysis;
  - Normalization;
  - Expression measures.

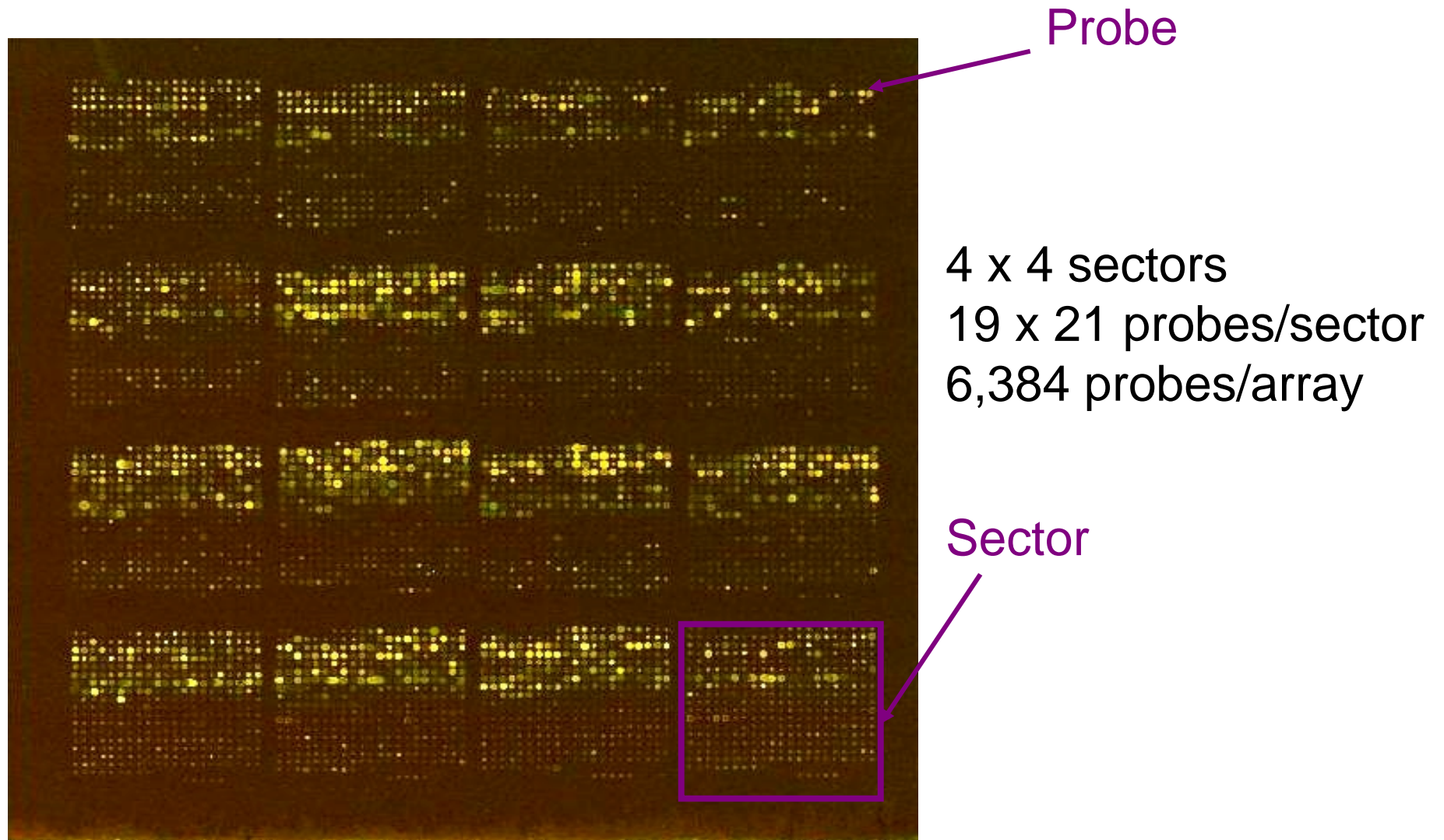
# cDNA microarrays



# Terminology

- **Target:** DNA hybridized to the array, mobile substrate.
- **Probe:** DNA spotted on the array, aka. spot, immobile substrate.
- **Sector:** collection of spots printed using the same print-tip (or pin), aka. **print-tip-group**, pin-group, spot matrix, grid.
- The terms **slide** and **array** are often used to refer to the printed microarray.
- **Batch:** collection of microarrays with the same probe layout.
- **Cy3 = Cyanine 3 = green dye.**
- **Cy5 = Cyanine 5 = red dye.**

# RGB overlay of Cy3 and Cy5 images

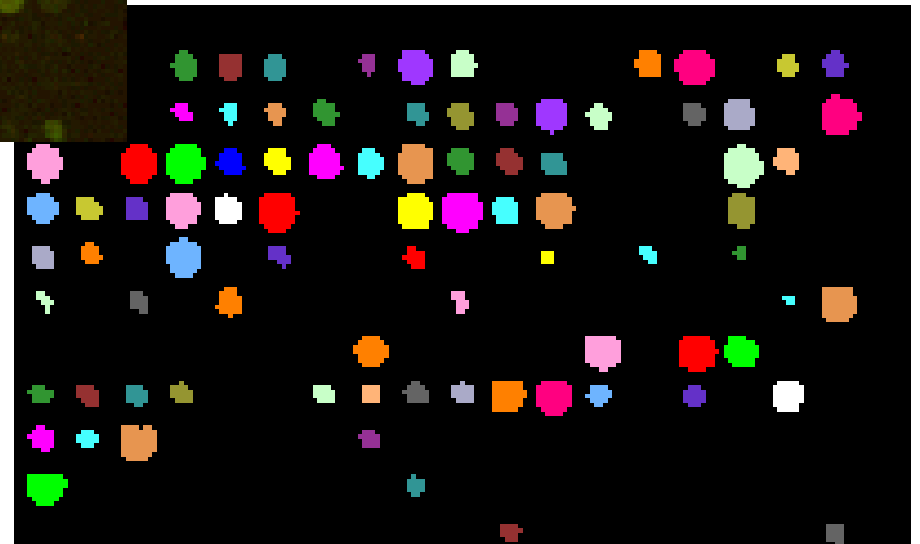
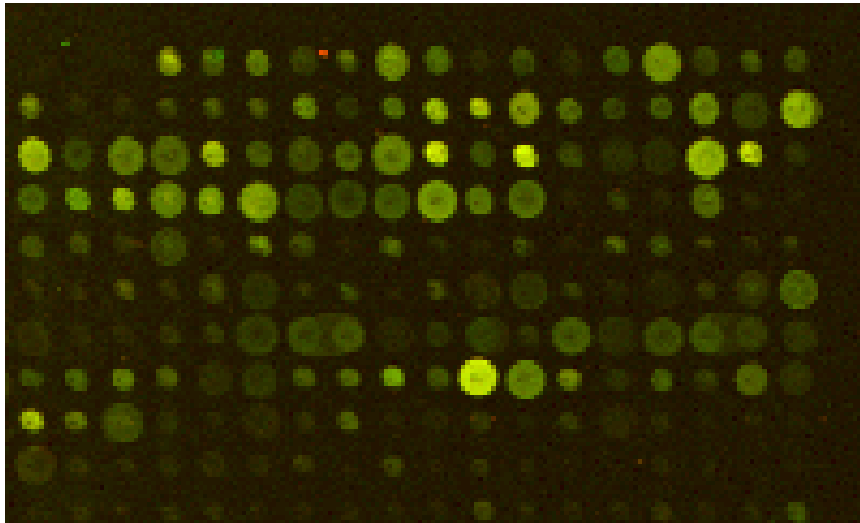


# Raw data

E.g. Human cDNA arrays

- ~43K spots;
- 16-bit TIFFs: ~ 20Mb per channel;
- ~ 2,000 x 5,500 pixels per image;
- Spot separation: ~ 136 $\mu$ m;
- For a “typical” array, the spot area has
  - mean = 43 pixels,
  - med = 32 pixels,
  - SD = 26 pixels.

# Image analysis



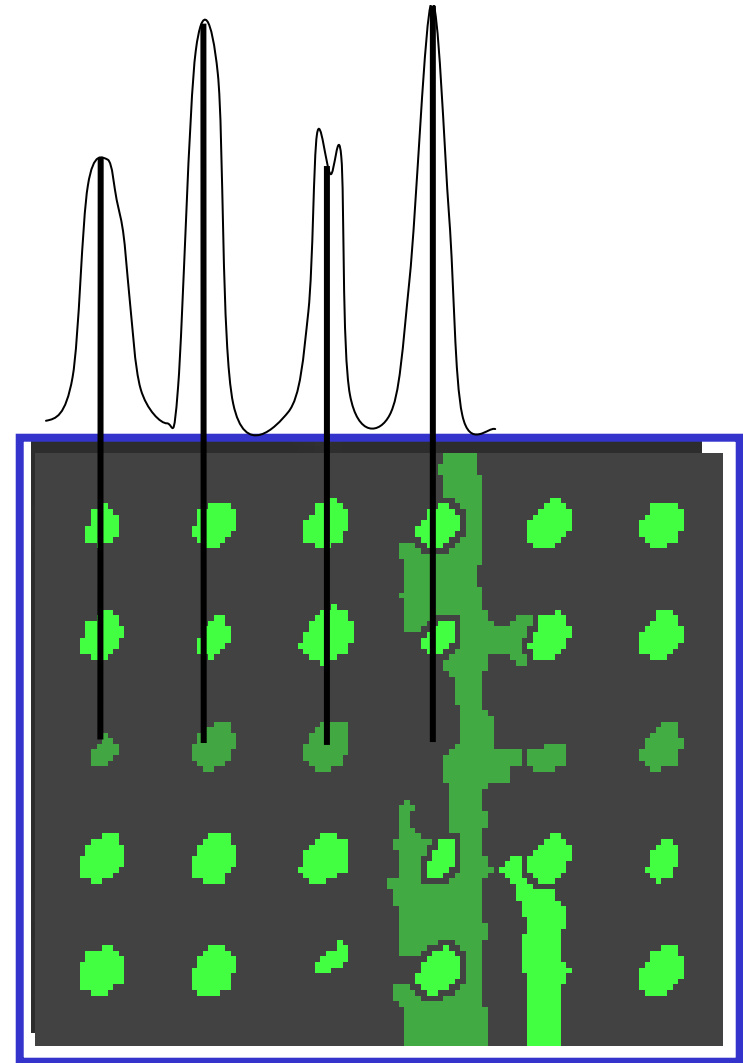


# Image analysis

- The **raw data** from a cDNA microarray experiment consist of pairs of **image files**, 16-bit TIFFs, one for each of the dyes.
- **Image analysis** is required to extract measures of the red and green fluorescence intensities, **R** and **G**, for each spot on the array.

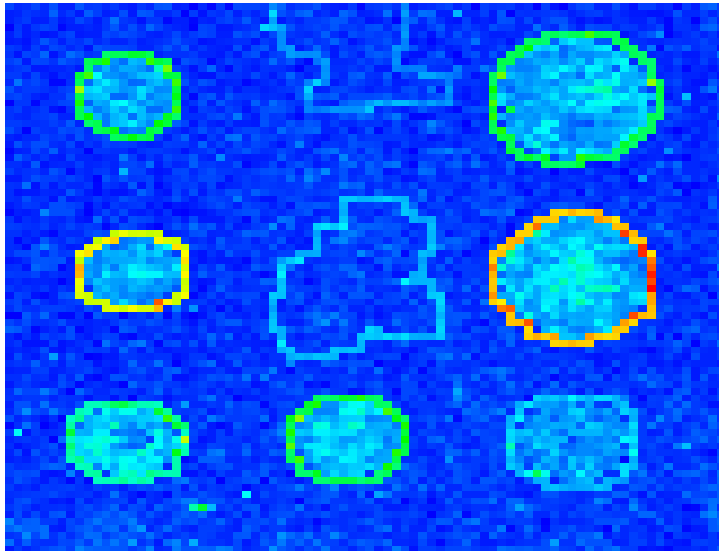
# Image analysis

- 1. Addressing.** Estimate location of spot centers.
- 2. Segmentation.** Classify pixels as foreground (signal) or background.
- 3. Information extraction.** For each spot on the array and each dye
  - foreground intensities;
  - background intensities;
  - quality measures.

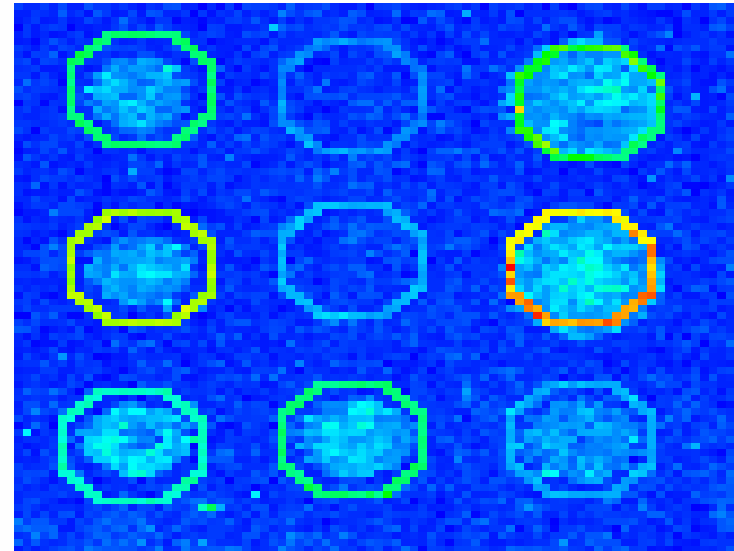


→ **R** and **G** for each spot on the array.

# Segmentation



Adaptive segmentation, SRG



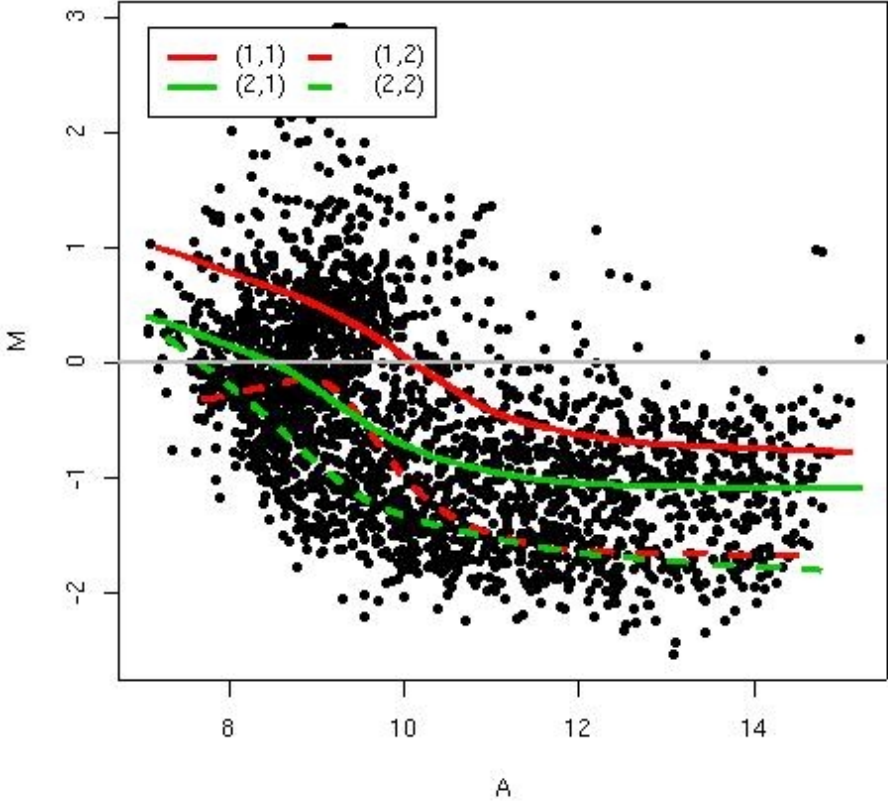
Fixed circle segmentation

**Spots usually vary in size and shape.**

# Quality measures

- **Spot quality**
  - **Brightness:** foreground/background ratio;
  - **Uniformity:** variation in pixel intensities and ratios of intensities within a spot;
  - **Morphology:** area, perimeter, circularity.
- **Slide quality**
  - Percentage of spots with no signal;
  - Range of intensities;
  - Distribution of spot signal area, etc.
- How to use quality measures in subsequent analyses?

# Normalization



# Normalization

- **Purpose.** Identify and remove the effects of **systematic variation** in the measured fluorescence intensities, other than differential expression, for example
  - different labeling efficiencies of the dyes;
  - different amounts of Cy3- and Cy5-labeled mRNA;
  - different scanning parameters;
  - print-tip, spatial, or plate effects, etc.

# Normalization

- Normalization is needed to ensure that differences in intensities are indeed due to differential expression, and not some printing, hybridization, or scanning artifact.
- Normalization is necessary before any analysis which involves within or between slides comparisons of intensities, e.g., clustering, testing.

# Normalization

- The need for normalization can be seen most clearly in **self-self hybridizations**, where the same mRNA sample is labeled with the Cy3 and Cy5 dyes.
- The imbalance in the red and green intensities is usually **not constant** across the spots within and between arrays, and can vary according to overall spot intensity, location, plate origin, etc.
- These factors should be considered in the normalization.

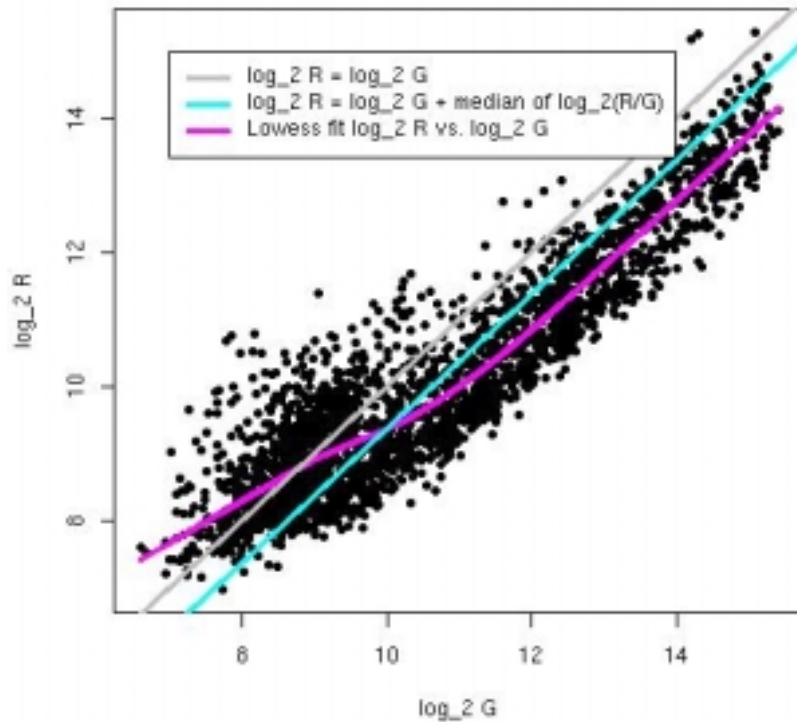


# Single-slide data display

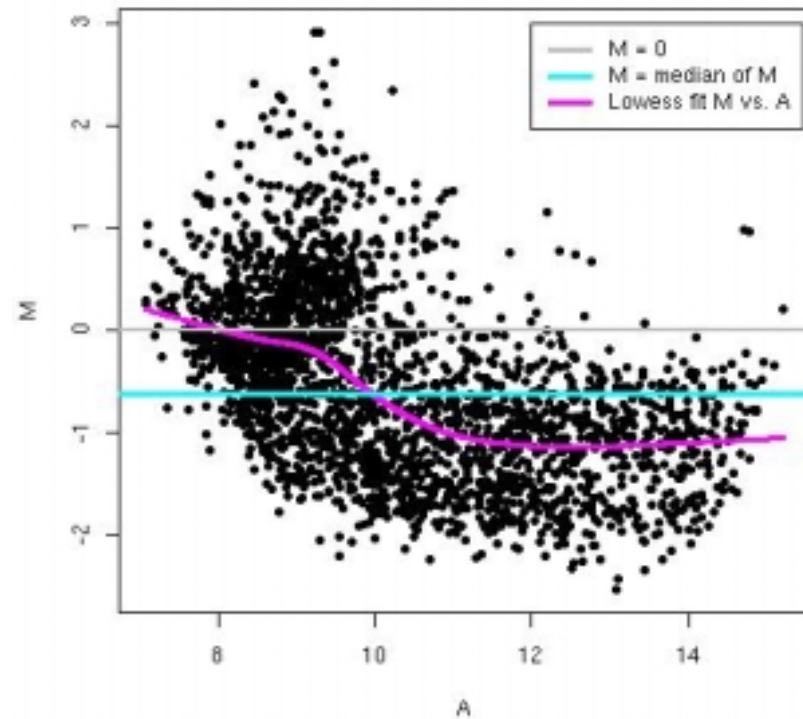
- Usually: R vs. G  
 $\log_2 R$  vs.  $\log_2 G$ .
- Preferred  
 $M = \log_2 R - \log_2 G$   
vs.  $A = (\log_2 R + \log_2 G)/2$ .
- An MA-plot amounts to a  $45^\circ$  counterclockwise rotation of a  $\log_2 R$  vs.  $\log_2 G$  plot followed by scaling.

# Self-self hybridization

$\log_2 R$  vs.  $\log_2 G$



M vs. A

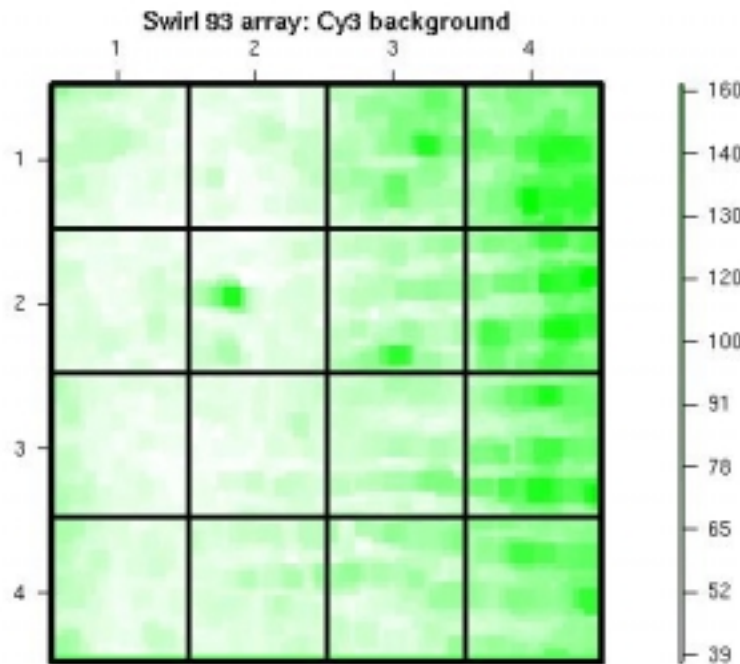


$$M = \log_2 R - \log_2 G, \quad A = (\log_2 R + \log_2 G)/2$$

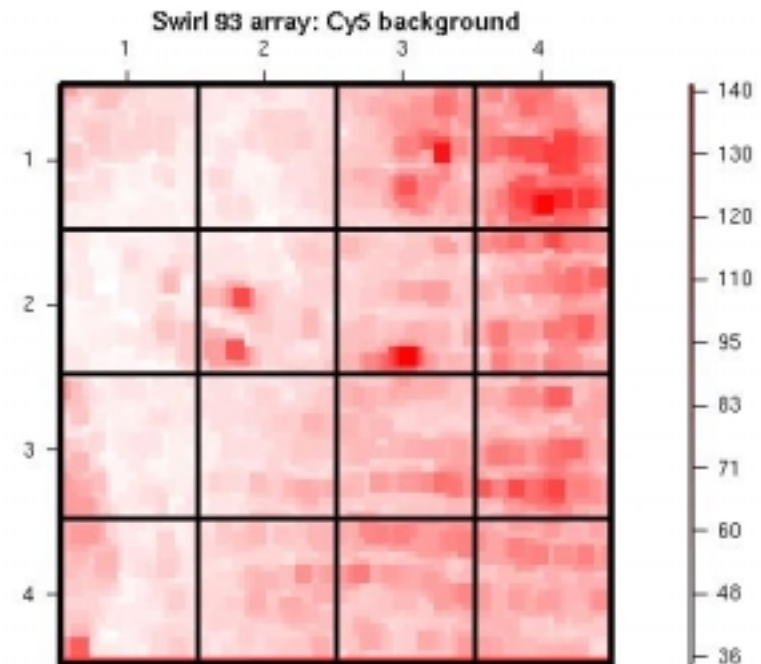
# Diagnostic plots

- **Diagnosics plots** of spot statistics  
E.g. red and green log-intensities, intensity log-ratios  $M$ , average log-intensities  $A$ , spot area.
  - Boxplots;
  - 2D spatial images;
  - Scatter-plots, e.g. MA-plots;
  - Density plots.
- **Stratify** plots according to layout parameters, e.g. print-tip-group, plate.

# 2D spatial images



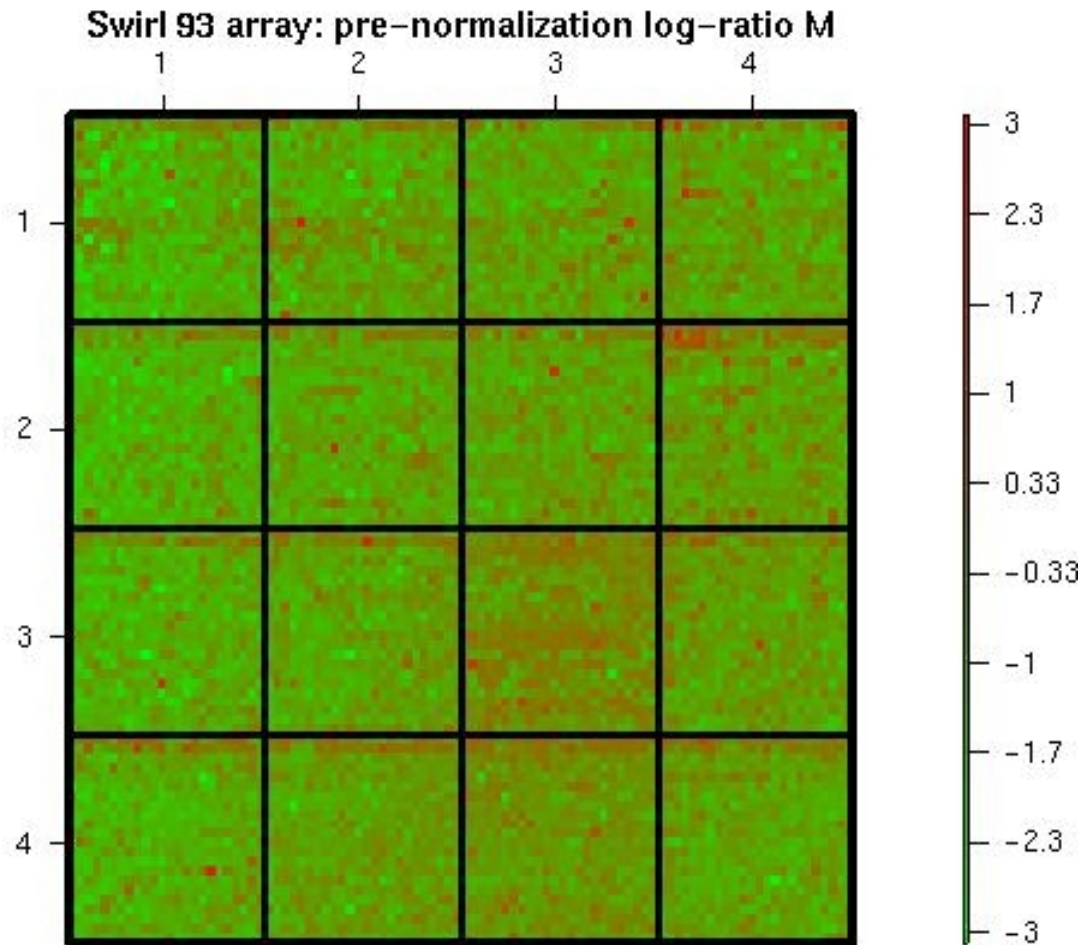
**Cy3 background intensity**



**Cy5 background intensity**

# 2D spatial images

Intensity  
log-ratio, M

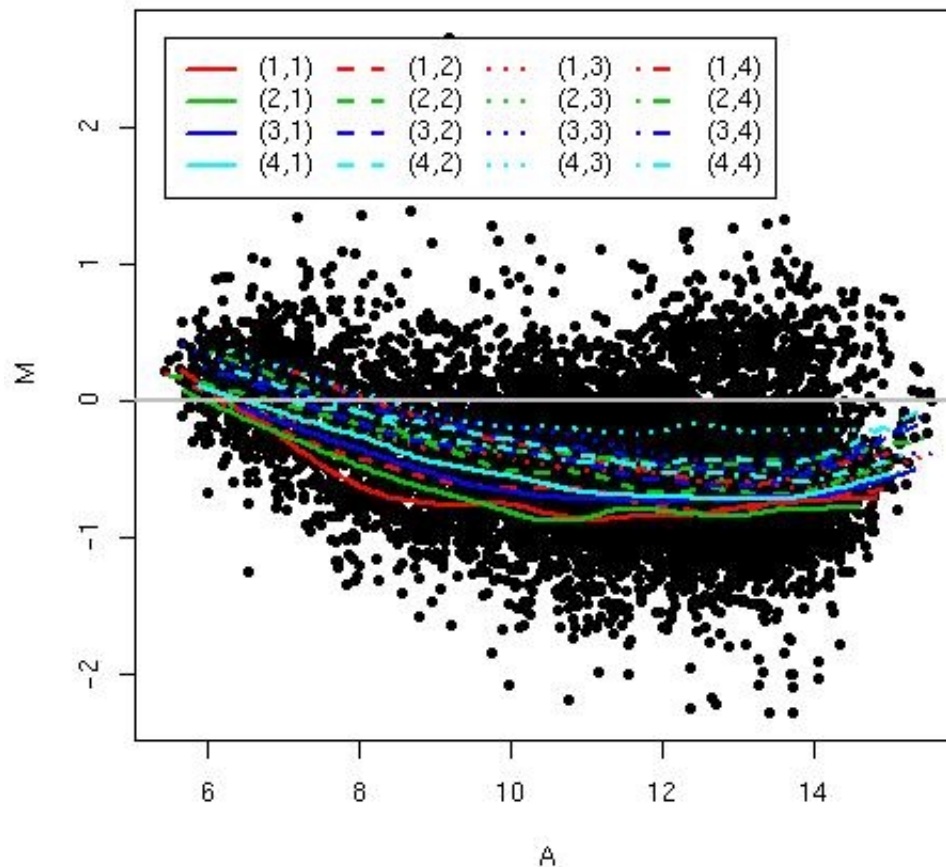


# MA-plot by print-tip-group

$$M = \log_2 R - \log_2 G, \quad A = (\log_2 R + \log_2 G)/2$$

Swirl 93 array: pre-normalization log-ratio M

Intensity  
log-ratio, M



Average  
log-intensity, A

# Location normalization

$$\log_2 R/G \leftarrow \log_2 R/G - L(\text{intensity, sector, ...})$$

- **Constant normalization.** Normalization function  $L$  is **constant** across the spots, e.g. mean or median of the log-ratios  $M$ .
- **Adaptive normalization.** Normalization function  $L$  depends on a number of **predictor variables**, such as spot intensity  $A$ , sector, plate origin.

# Location normalization

- The normalization function can be obtained by **robust locally weighted regression** of the log-ratios  $M$  on predictor variables.

E.g. regression of  $M$  on  $A$  within sector.

- Regression method: e.g. lowess or loess (Cleveland, 1979; Cleveland & Devlin, 1988).

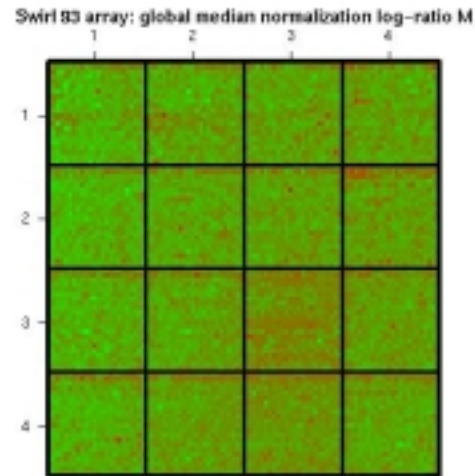


# Location normalization

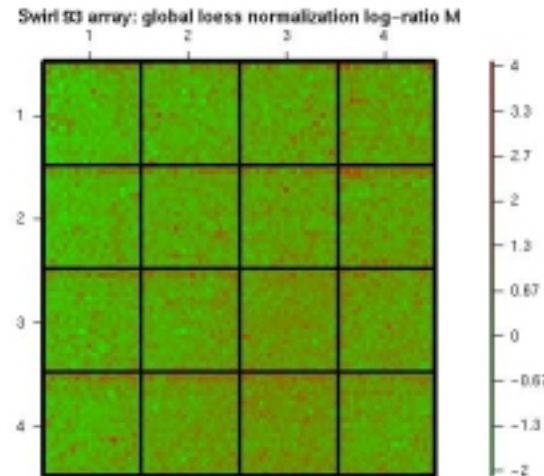
- **Intensity-dependent normalization.**  
Regression of  $M$  on  $A$  (*global loess*).
- **Intensity and sector-dependent normalization.**  
Same as above, for each sector separately (*within-print-tip-group loess*).
- **2D spatial normalization.**  
Regression of  $M$  on 2D-coordinates.
- Other variables: time of printing, plate, etc.
- **Composite normalization.** Weighted average of several normalization functions.

# 2D images of normalized M-L

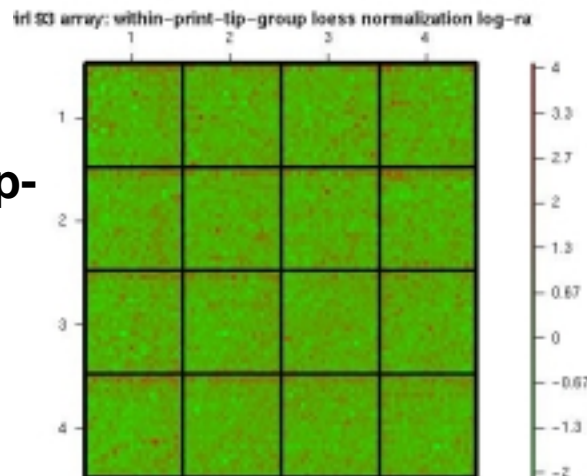
**Global median normalization**



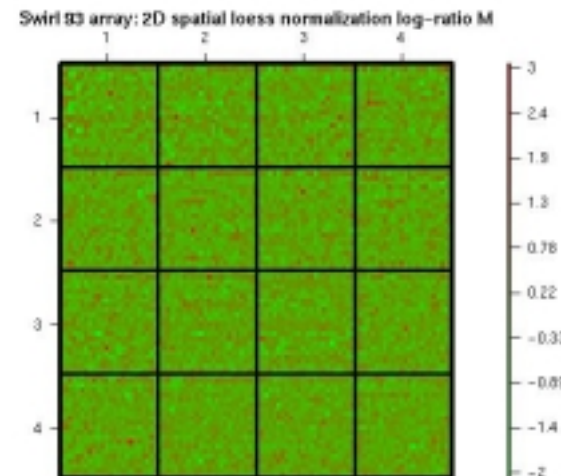
**Global loess normalization**



**Within-print-tip-group loess normalization**

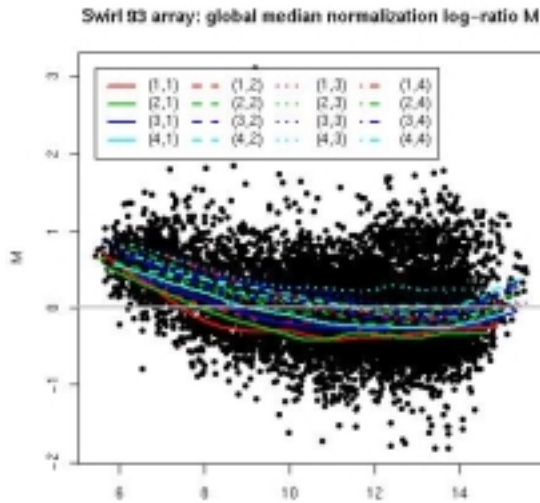


**2D spatial normalization**

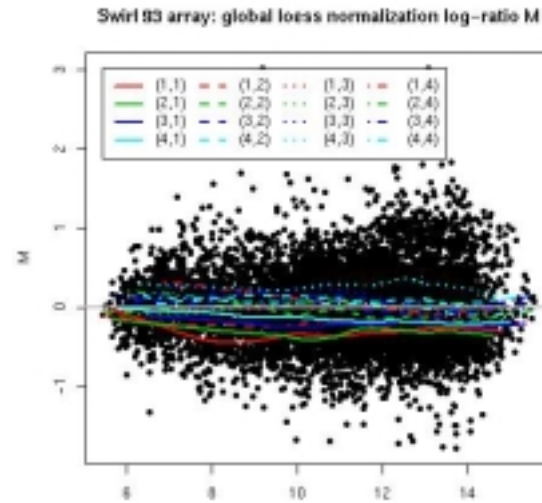


# MA-plots of normalized M-L

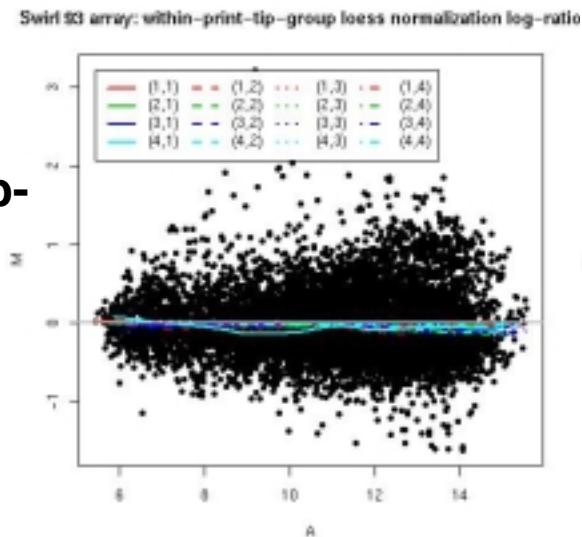
**Global median normalization**



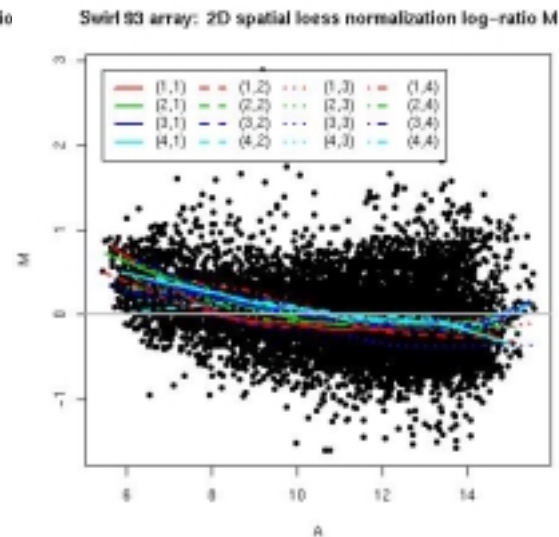
**Global loess normalization**



**Within-print-tip-group loess normalization**



**2D spatial normalization**



# Normalization

- Within-slide
  - **Location** normalization - additive on log-scale.
  - **Scale** normalization - multiplicative on log-scale.
  - **Which spots** to use?
- Paired-slides (dye-swap experiments)
  - Self-normalization.
- Between-slides.

# Scale normalization

- The log-ratios  $M$  from different sectors, plates, or arrays may exhibit different spreads and some **scale** adjustment may be necessary.

$$\log_2 R/G \leftarrow (\log_2 R/G - L)/S$$

- Can use a robust estimate of scale such as the **median absolute deviation (MAD)**  
 $MAD = \text{median} | M - \text{median}(M) |.$

# Scale normalization

- For print-tip-group scale normalization, assume all print-tip-groups have the same spread in  $M$ .
- Denote **true** and **observed** log-ratio by  $\mu_{ij}$  and  $M_{ij}$ , resp. Robust estimate of  $\mu_{ij}$  is  $\hat{a}_i = \frac{MAD_i}{\sqrt[3]{\prod_{i=1}^I MAD_i}}$  and  $i$  indexes print-tip-group and  $j$  spots.

where  $MAD_i$  is MAD of  $M_{ij}$  in print-tip-group

# Algorithm Median Absolute Deviation (MAD) scale normalization

**Input:** log intensity ratios  $M_j = \log_2 R_j/G_j$  for the overall genes in a given slide or within a given print-tip-group,  $1 \leq j \leq n$

**Output:** scale normalization factor for a given slide  $S$  or a print-tip-group  $S_i$

1.  $m = \text{median}_j (M_j)$
2.  $AD = \{ ad_j = |m_j - m|, 1 \leq j \leq n \}$
3.  $MAD = \text{median}_j (ad_j)$
4. Output:

A. Within slide:

$$S = MAD$$

B. Within print-tip-group:

$$S_i = \frac{MAD_i}{\sqrt[I]{\prod_{i=1}^I MAD_i}}$$

# Which genes to use?

- **All spots on the array:**
  - Problem when many genes are differentially expressed.
- **Housekeeping genes:** Genes that are thought to be constantly expressed across a wide range of biological samples (e.g. tubulin, GAPDH).

Problems:

  - sample specific biases (genes are actually regulated),
  - do not cover intensity range.



# Which genes to use?

- **Genomic DNA titration series:**
  - fine in yeast,
  - but weak signal for higher organisms with high intron/exon ratio (e.g. mouse, human).
- **Rank invariant set** (Schadt et al., 1999; Tseng et al., 2001): genes with same rank in both channels. Problems: set can be small.

# Microarray sample pool

- **Microarray Sample Pool, MSP**: Control sample for normalization, in particular, when it is not safe to assume most genes are equally expressed in both channels.
- MSP: **pooled** all 18,816 ESTs from RIKEN release 1 cDNA mouse library.
- Six-step **dilution series** of the MSP.
- MSP samples were spotted in middle of first and last row of each sector.
- Ref. Yang et al. (2002).

# Microarray sample pool

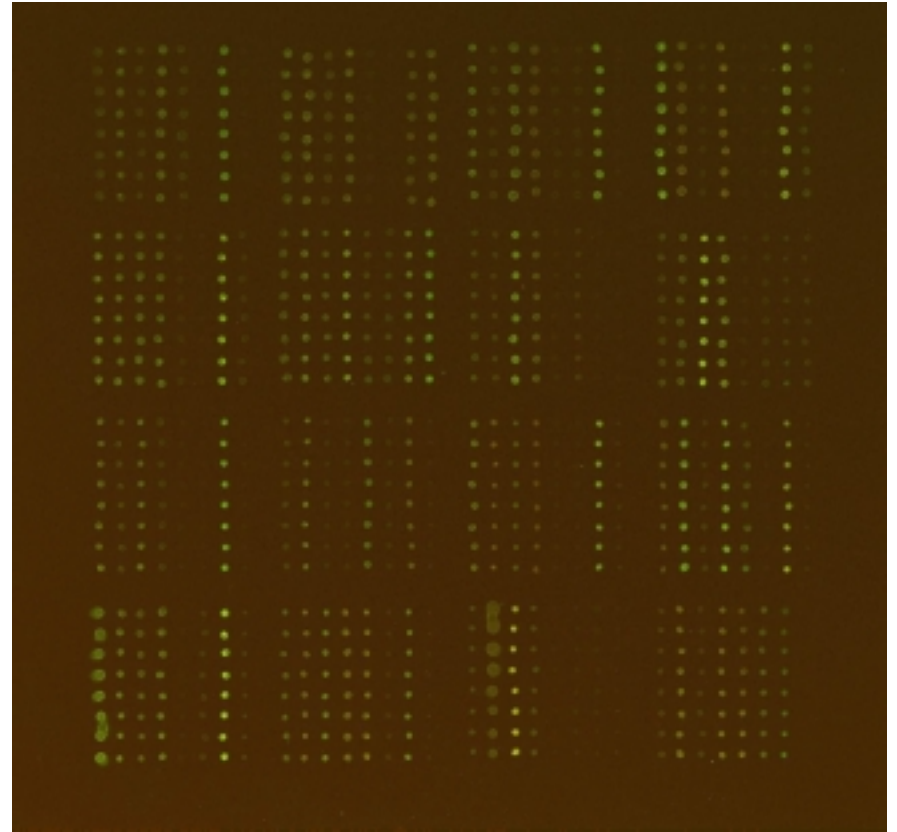
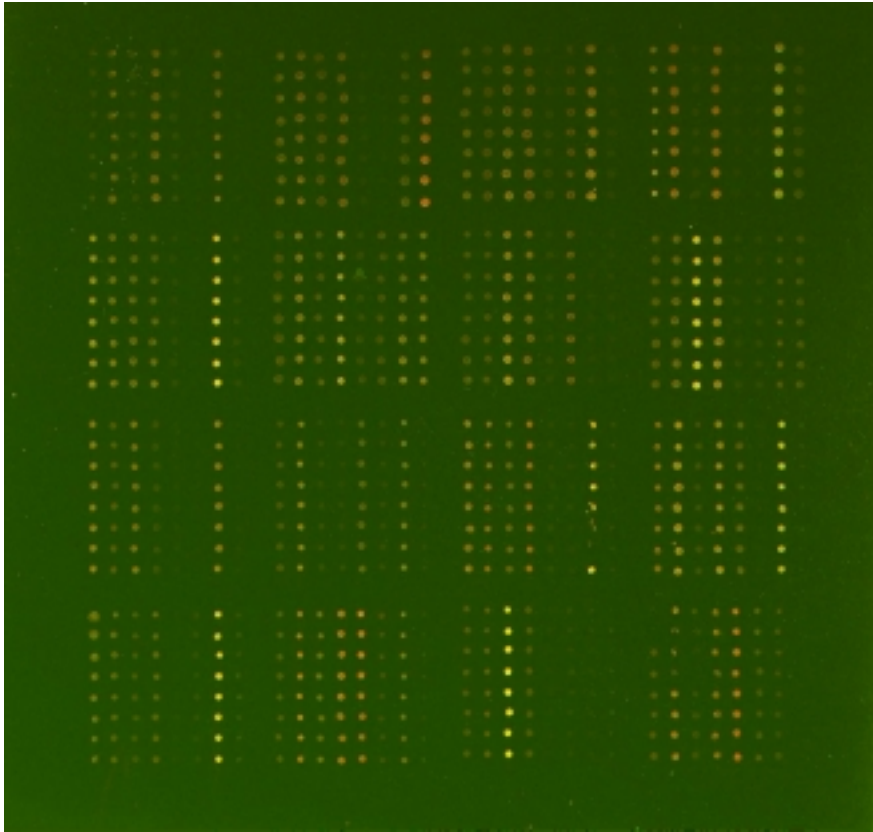
## MSP control spots

- provide potential probes for every target sequence;
- are constantly expressed across a wide range of biological samples;
- cover the intensity range;
- are similar to genomic DNA, but without intron sequences → better signal than genomic DNA in organisms with high intron/exon ratio;
- can be used in composite normalization.

# Dye-swap experiment

- Probes
  - 50 distinct clones thought to be differentially expressed in apo AI knock-out mice compared to inbred C57Bl/6 control mice (largest absolute t-statistics in a previous experiment).
  - 72 other clones.
- Spot each clone 8 times .
- Two hybridizations with dye-swap:
  - Slide 1: trt → red,      ctl → green.
  - Slide 2: trt → green,    ctl → red.

# Dye-swap experiment



# Self-normalization

- Slide 1,  $M = \log_2 (R/G) - L$
- Slide 2,  $M' = \log_2 (R'/G') - L'$

Combine by **subtracting** the normalized log-ratios:

$$M - M'$$

$$= [ (\log_2 (R/G) - L) - (\log_2 (R'/G') - L') ] / 2$$

$$\approx [ \log_2 (R/G) + \log_2 (G'/R') ] / 2$$

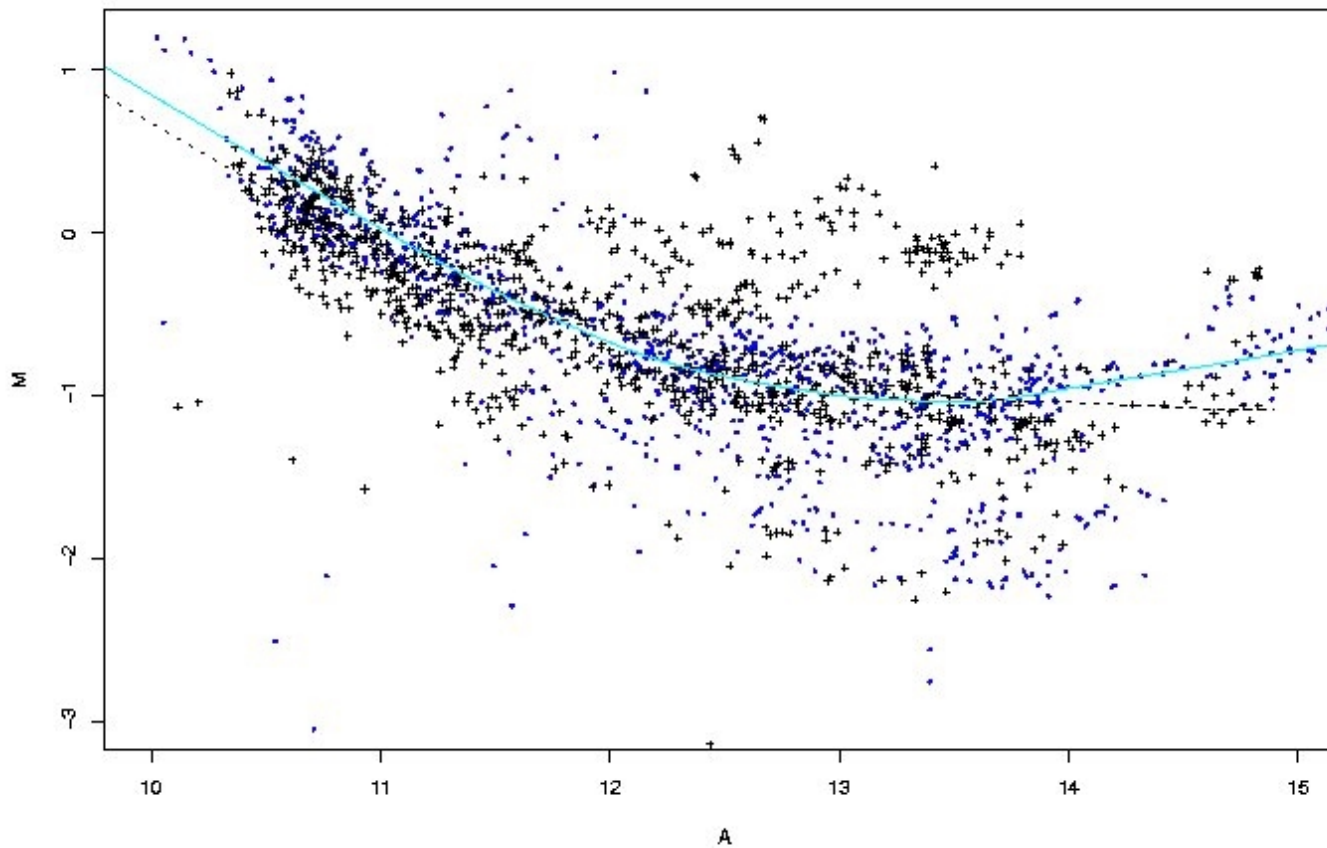
$$\approx [ \log_2 (RG'/GR') ] / 2$$

provided  $L = L'$ .

***Assumption: the normalization functions are the same for the two slides.***

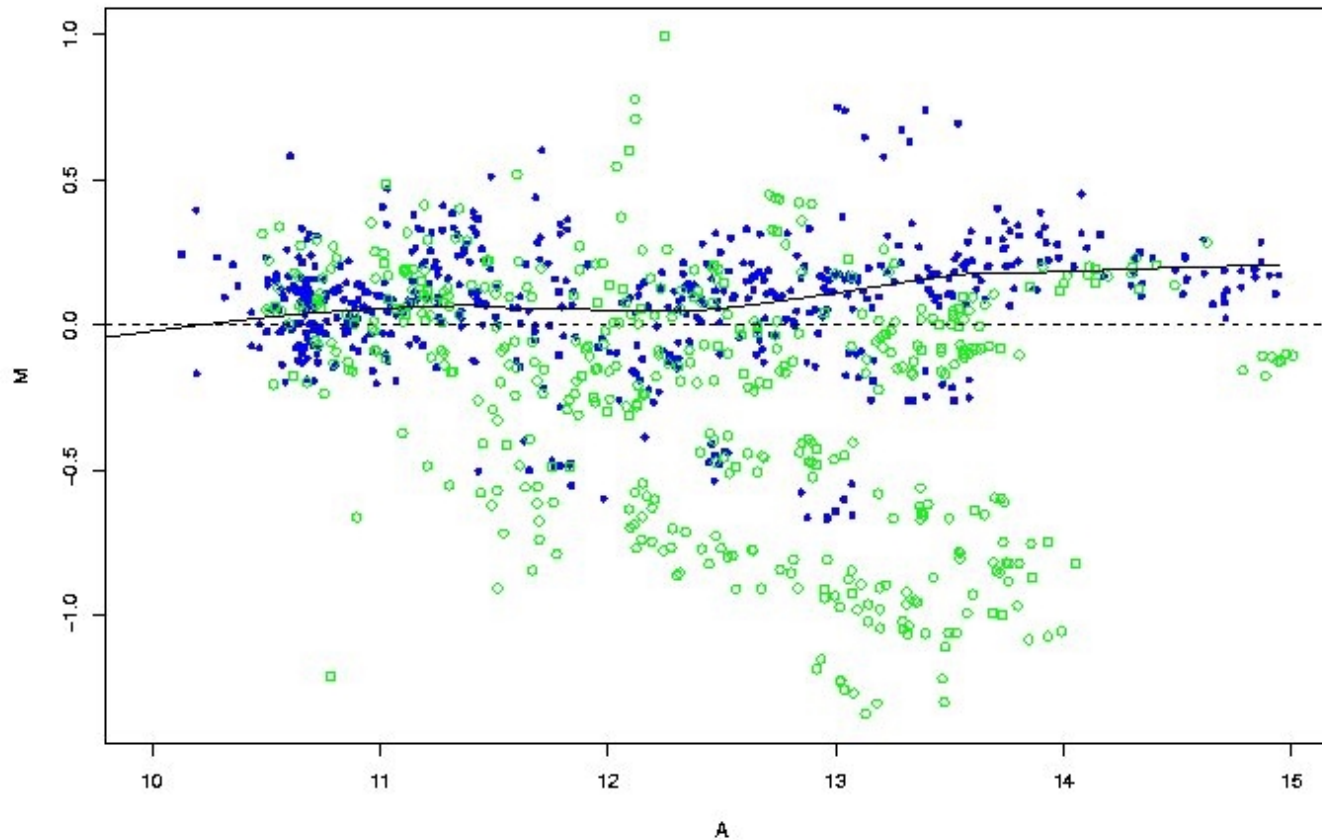
# Checking the assumption

## MA-plot for slides 1 and 2



# Result of self-normalization

$(M - M')/2$  vs.  $(A + A')/2$





# Summary

Case 1. Only a few genes are expected to change.

Within-slide

- Location: intensity + sector-dependent normalization.
- Scale: for each sector, scale by MAD.

Between-slides

- An extension of within-slide scale normalization.

Case 2. Many genes are expected to change.

- Paired-slides: Self-normalization.
- Use of controls or known information, e.g. MSP.
- Composite normalization.