

# Intensity transformations

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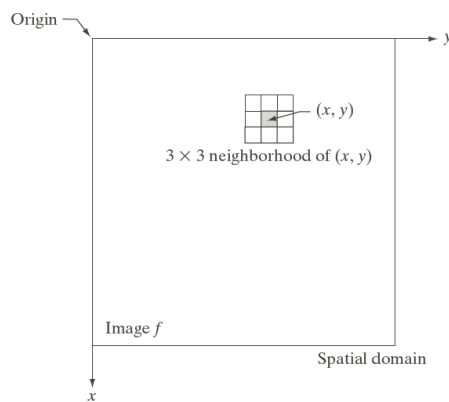
## Methods for Image Processing

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### Spatial domain

- ▶ The *spatial domain* of an image is the plane that contains the image pixels.
- ▶ The techniques that operate on the spatial domain make direct use of the information contained into the matricial representation of the image;
  - ▶ in contrast to other techniques that operate onto representation of the image in other domains (which is computed through a suitable transform).
- ▶ This kind of techniques can be formalized as:
$$g(x, y) = T[f(x, y)]$$
- ▶ Generally, spatial domain techniques are less computationally demanding.

## Transformations in the spatial domain

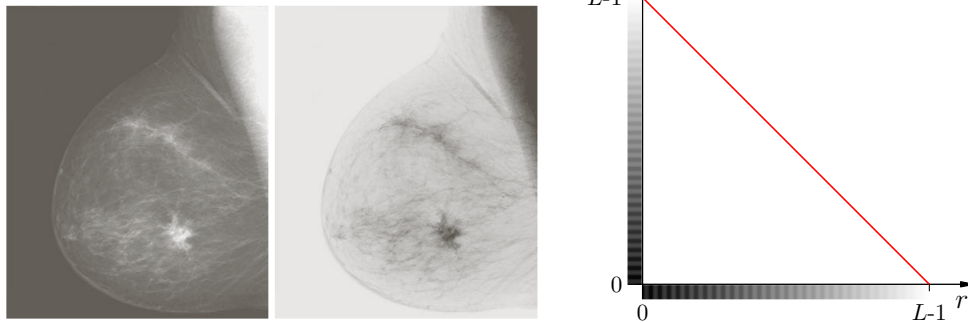


- ▶ The operator,  $T$ , is usually defined on a suitable neighborhood of  $(x, y)$ .
  - ▶ A rectangular neighborhood is usually preferred.
  - ▶ When the neighborhood fall outside the image, some extending criteria have to be used
    - ▶ background-padding
    - ▶ zero-padding
    - ▶ symmetry
- ▶ If the radius of the neighborhood is 0, the transformation involves only the considered pixel and depends (only) by its intensity:
  - ▶  $s = T(r)$
  - ▶ intensity transformation or gray-level mapping.

## Intensity transformations

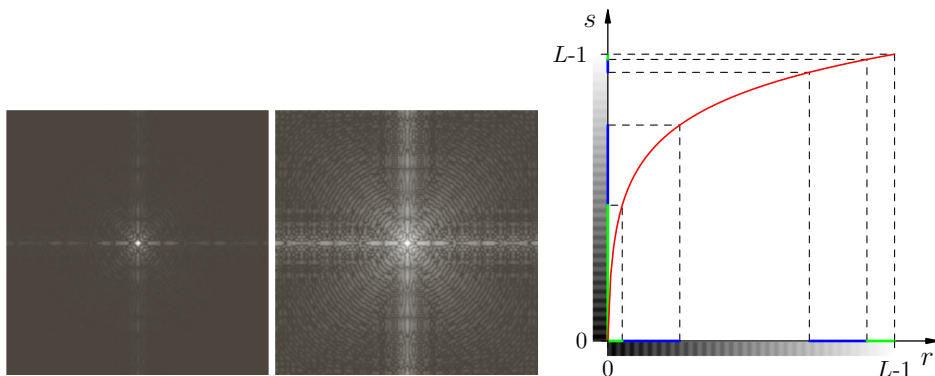
- ▶ Intensity transformation techniques are also called *point-processing*, as opposed to the *neighborhood processing* techniques.
- ▶ Simple to implement (algorithm, table map).
- ▶ They are used to enhance images that are devoted to visual processing:
  - ▶ no general rule for stating the optimality;
  - ▶ application-dependent;
  - ▶ user-dependent.

## Image negative



- ▶ Sometimes, the details are more detectable when the pixels intensity is reversed.
  - ▶ For instance, when the details are white or light gray and the background is dark and covers the most of the image.
- ▶  $s = L - 1 - r$

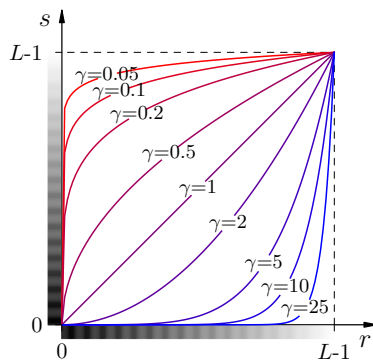
## Logarithmic transformations



- ▶  $s = c \log(1 + r), \quad c = \frac{L-1}{\log L}$
- ▶ Useful for representing bidimensional functions that are defined on large intervals and have high and small peaks.
  - ▶ e.g.:  $f : [0, 1]^2 \rightarrow [0, 10^6]$

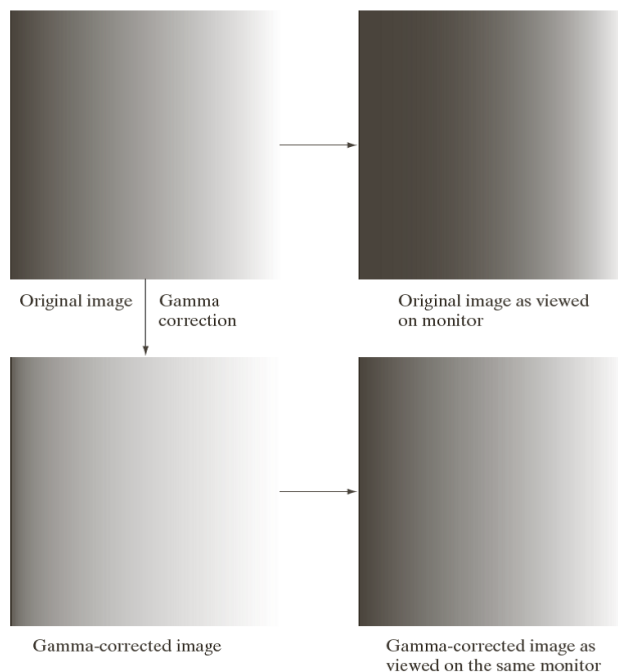
## Gamma transformations

- ▶ Also called *power-law* transformations.
- ▶  $s = c r^\gamma$  (sometimes  $s = c (r + \epsilon)^\gamma$ )
- ▶ Used for correcting the visualization devices output.
- ▶ Useful for contrast correction (or enhancement).
- ▶ A too large or too small value for  $\gamma$  can compromise the results.



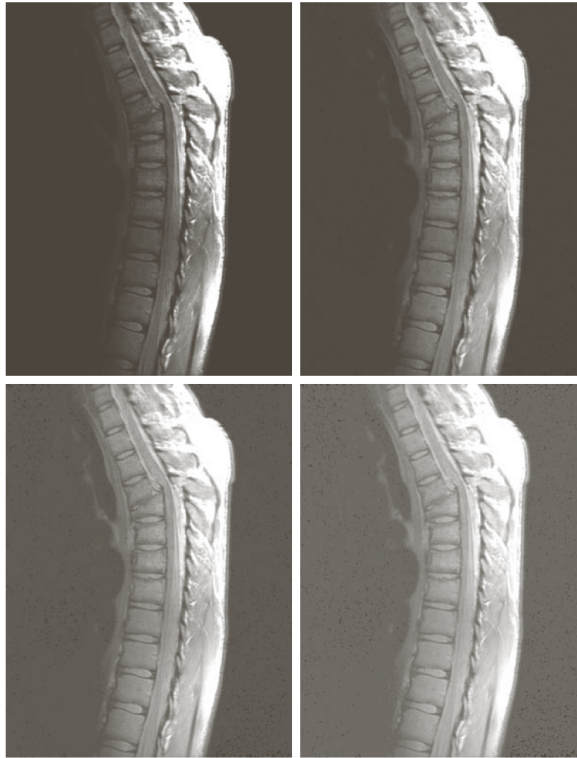
- ▶  $\gamma = 1$ , identity
- ▶  $\gamma < 1$ , lightening
- ▶  $\gamma > 1$ , darkening

## Gamma transformations (2)



If the gamma correction factor of the average visualization device is known in advance, a suitable correction can be applied to the image intensity before the visualization.

### Gamma transformations (3)



a	b
c	d

(a) Original image.

Gamma transformed images with

$c = 1, \gamma = 0.6$  (b),

$c = 1, \gamma = 0.4$  (c),

and  $c = 1, \gamma = 0.3$  (d).

Which is the best?

### Gamma transformations (4)



a	b
c	d

Gamma correction can be applied also for darkening images.

(a) Original image.

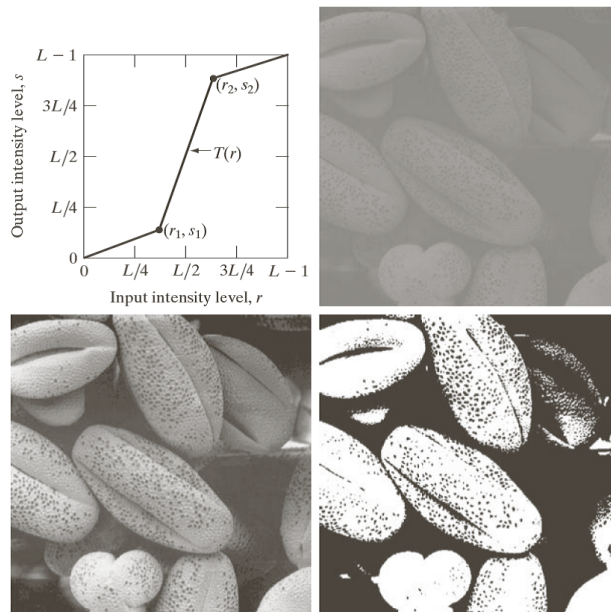
Gamma transformed images with

$c = 1, \gamma = 3.0$  (b),

$c = 1, \gamma = 4.0$  (c),

and  $c = 1, \gamma = 5.0$  (d).

## Contrast stretching transformations



a	b
c	d

(a) General shape of the contrast stretching transformations.

(b) Low-contrast image.

(c) A processed image.

$$(r_1, s_1) = (r_{\min}, 0)$$

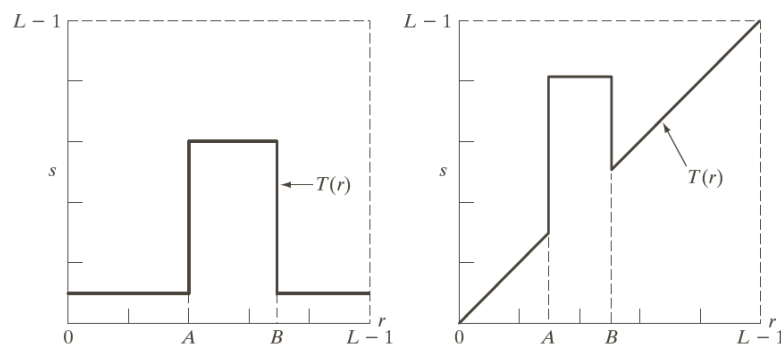
$$(r_2, s_2) = (r_{\max}, L - 1)$$

(d) Thresholding can be view as the limit of the contrast stretching.

$$(r_1, s_1) = (r_{\text{thr}}, 0)$$

$$(r_2, s_2) = (r_{\text{thr}}, L - 1)$$

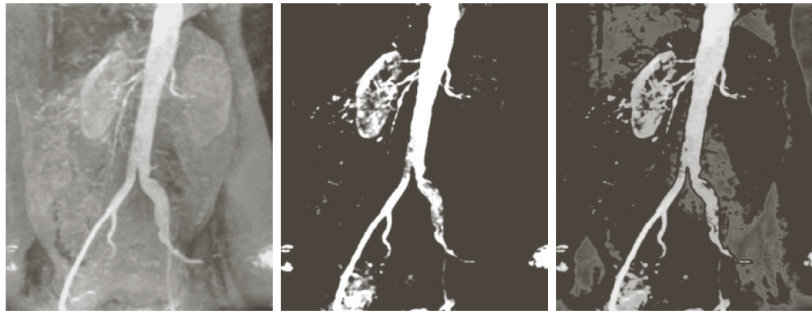
## Intensity level slicing transformations



a | b

- Intensity level slicing transformations highlight an intensity range.
- The transformation in (a) sets all the intensities that are not in  $[A, B]$  to a low value.
- The transformation in (b) preserves the intensities that are not in  $[A, B]$ .

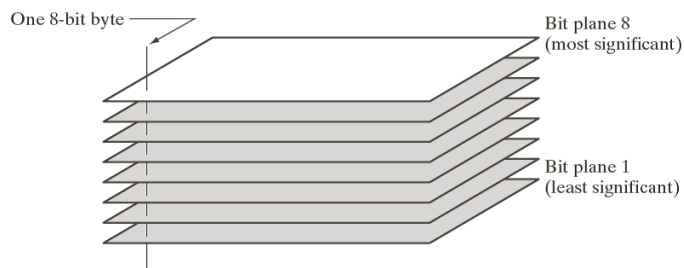
## Intensity level slicing transformations (2)



a | b | c

- ▶ (a) Original image.
- ▶ (b) Vessels are highlighted by setting to  $L - 1$  the intensity levels that are in the range of interest and to 0 all the others.
- ▶ (c) Vessels intensities are conserved, while the others are darkened.

## Bit-plane transformation



- ▶ Instead of considering it as a matrix of integer, the image can be seen as composed of layers of bits.



## Bit-plane transformation (2)



- Each layer contributes to the final appearance of the image, but most of the information is in the higher layers.



## Bit-plane transformation (3)



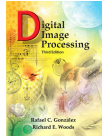
a  
b  
c

Images obtained using:

- (a) bitplanes 8 and 7;
- (b) bitplanes 8, 7, and 6;
- (c) bitplanes 8, 7, 6, and 5.



## Homeworks and suggested readings



DIP, Sections 3.1, 3.2

- ▶ pp. 105–119



GIMP

- ▶ Colors
  - ▶ Brightness-Contrast
  - ▶ Threshold
  - ▶ Levels
  - ▶ Curves
  - ▶ Invert
  - ▶ Auto
    - ▶ Stretch Contrast
    - ▶ Normalize