

Intensity transformations

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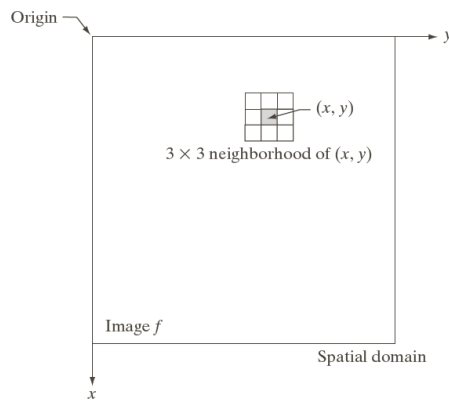
Methods for Image Processing

academic year 2014–2015

Spatial domain

- ▶ The *spatial domain* of an image is the plane that contains the image pixels.
- ▶ The techniques that operate on the spatial domain make direct use of the information contained into the matricial representation of the image;
 - ▶ in contrast to other techniques that operate onto representation of the image in other domains (which is computed through a suitable transform).
- ▶ This kind of techniques can be formalized as:
$$g(x, y) = T[f(x, y)]$$
- ▶ Generally, spatial domain techniques are less computationally demanding.

Transformations in the spatial domain

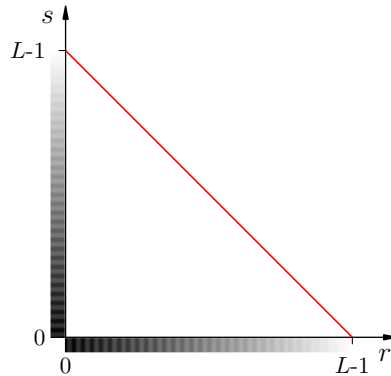
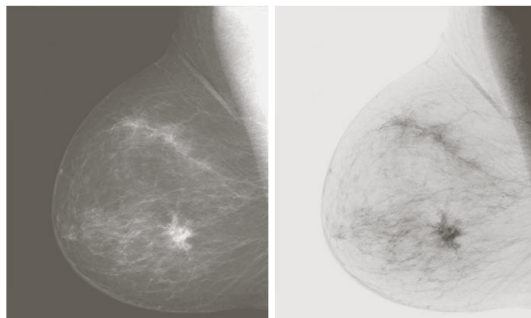


- ▶ The operator, T , is usually defined on a suitable neighborhood of (x, y) .
 - ▶ A rectangular neighborhood is usually preferred.
 - ▶ When the neighborhood fall outside the image, some extending criteria have to be used
 - ▶ background-padding
 - ▶ zero-padding
 - ▶ symmetry
- ▶ If the radius of the neighborhood is 0, the transformation involves only the considered pixel and depends (only) by its intensity:
 - ▶ $s = T(r)$
 - ▶ intensity transformation or gray-level mapping.

Intensity transformations

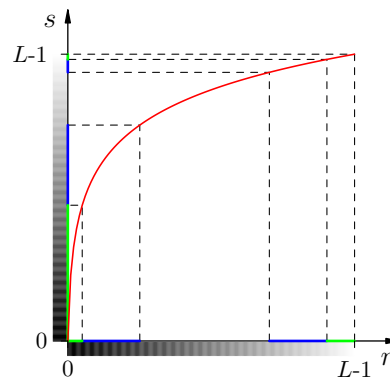
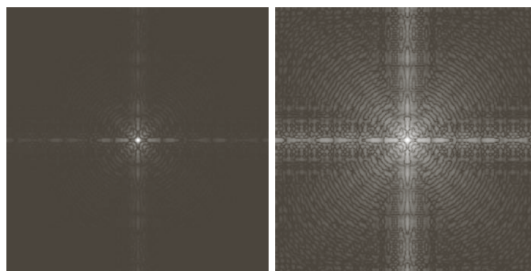
- ▶ Intensity transformation techniques are also called *point-processing*, as opposed to the *neighborhood processing* techniques.
- ▶ Simple to implement (algorithm, table map).
- ▶ They are used to enhance images that are devoted to visual processing:
 - ▶ no general rule for stating the optimality;
 - ▶ application-dependent;
 - ▶ user-dependent.

Image negative



- ▶ Sometimes, the details are more detectable when the pixels intensity is reversed.
 - ▶ For instance, when the details are white or light gray and the background is dark and covers the most of the image.
- ▶ $s = L - 1 - r$

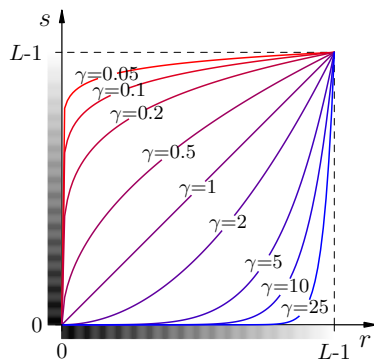
Logarithmic transformations



- ▶ $s = c \log(1 + r)$, $c = \frac{L-1}{\log L}$
- ▶ Useful for representing bidimensional functions that are defined on large intervals and have high and small peaks.
 - ▶ e.g.: $f : [0, 1]^2 \rightarrow [0, 10^6]$

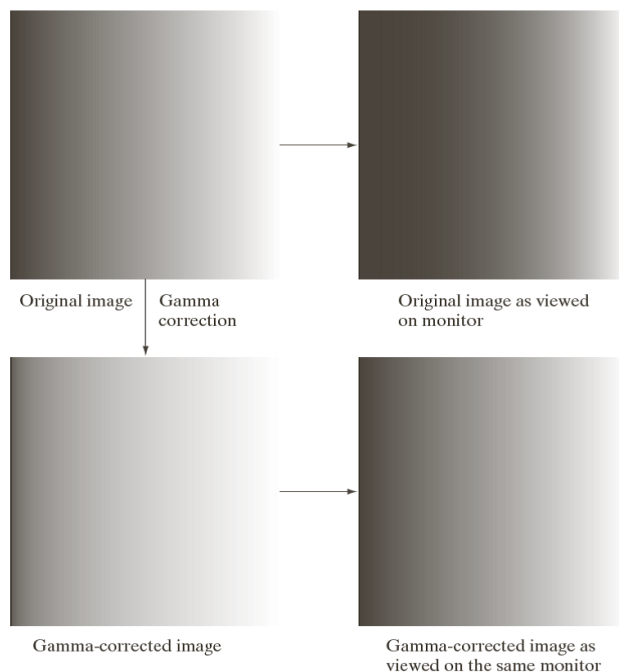
Gamma transformations

- ▶ Also called *power-law* transformations.
- ▶ $s = c r^\gamma$ (sometimes $s = c (r + \epsilon)^\gamma$)
- ▶ Used for correcting the visualization devices output.
- ▶ Useful for contrast correction (or enhancement).
- ▶ A too large or too small value for γ can compromise the results.



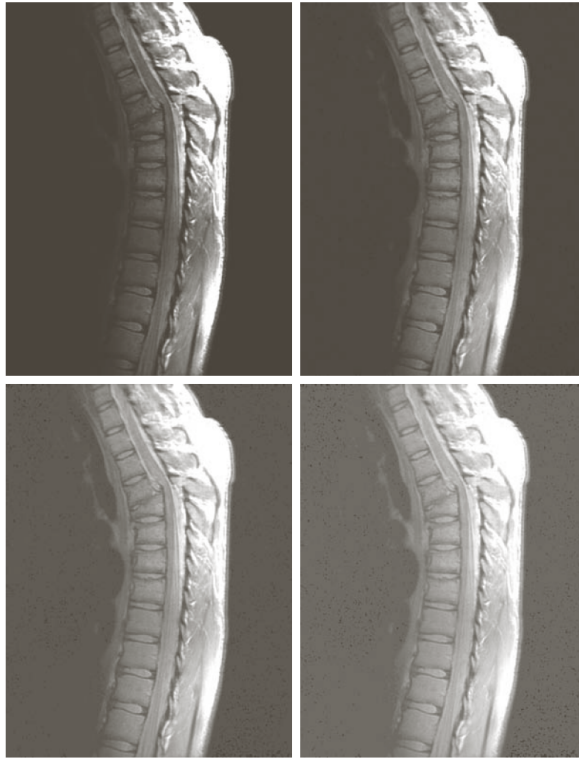
- ▶ $\gamma = 1$, identity
- ▶ $\gamma < 1$, lightening
- ▶ $\gamma > 1$, darkening

Gamma transformations (2)



If the gamma correction factor of the average visualization device is known in advance, a suitable correction can be applied to the image intensity before the visualization.

Gamma transformations (3)



a	b
c	d

(a) Original image.

Gamma transformed images with

$c = 1, \gamma = 0.6$ (b),

$c = 1, \gamma = 0.4$ (c),

and $c = 1, \gamma = 0.3$ (d).

Which is the best?

Gamma transformations (4)



a	b
c	d

Gamma correction can be applied also for darkening images.

(a) Original image.

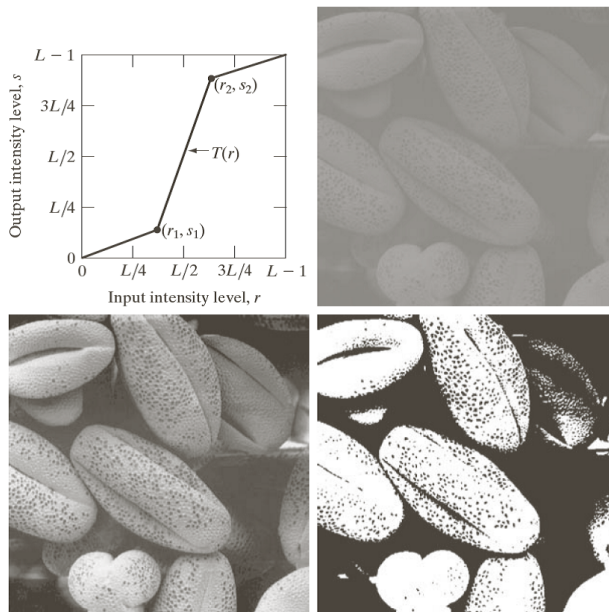
Gamma transformed images with

$c = 1, \gamma = 3.0$ (b),

$c = 1, \gamma = 4.0$ (c),

and $c = 1, \gamma = 5.0$ (d).

Contrast stretching transformations



$$\begin{array}{c|c} a & b \\ \hline c & d \end{array}$$

(a) General shape of the contrast stretching transformations.

(b) Low-contrast image.

(c) A processed image.

$$(r_1, s_1) = (r_{\min}, 0)$$

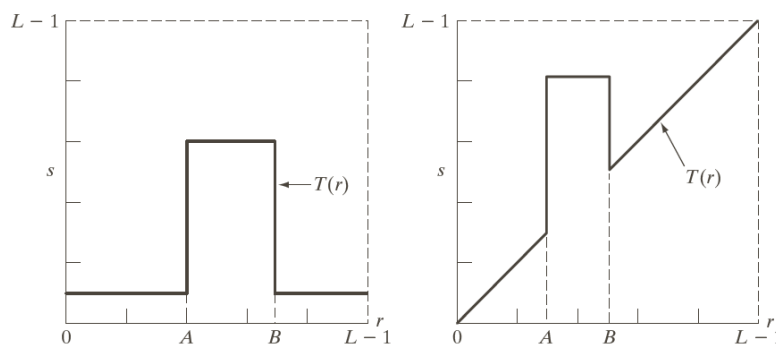
$$(r_2, s_2) = (r_{\max}, L - 1)$$

(d) Thresholding can be viewed as the limit of the contrast stretching.

$$(r_1, s_1) = (r_{\text{thr}}, 0)$$

$$(r_2, s_2) = (r_{\text{thr}}, L - 1)$$

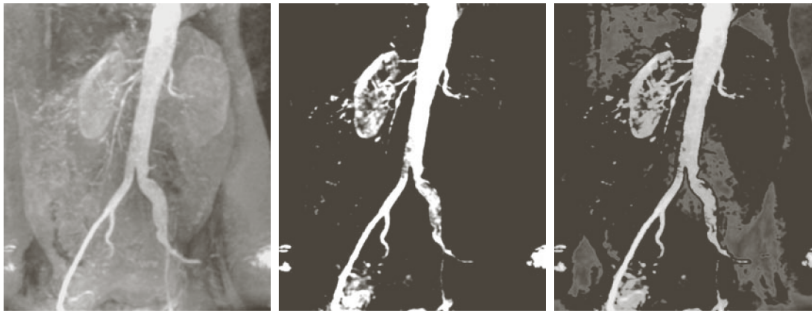
Intensity level slicing transformations



a | b

- ▶ Intensity level slicing transformations highlight an intensity range.
- ▶ The transformation in (a) sets all the intensities that are not in $[A, B]$ to a low value.
- ▶ The transformation in (b) preserves the intensities that are not in $[A, B]$.

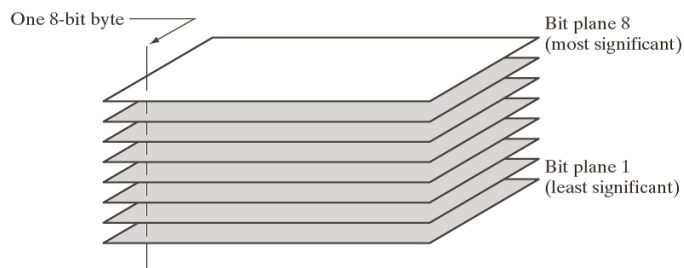
Intensity level slicing transformations (2)



a | b | c

- ▶ (a) Original image.
- ▶ (b) Vessels are highlighted by setting to $L - 1$ the intensity levels that are in the range of interest and to 0 all the others.
- ▶ (c) Vessels intensities are conserved, while the others are darkened.

Bit-plane transformation



- ▶ Instead of considering it as a matrix of integer, the image can be seen as composed of layers of bits.

Bit-plane transformation (2)



- ▶ Each layer contributes to the final appearance of the image, but most of the information is in the higher layers.



Bit-plane transformation (3)



a
b
c

Images obtained using:

- ▶ (a) bitplanes 8 and 7;
- ▶ (b) bitplanes 8, 7, and 6;
- ▶ (c) bitplanes 8, 7, 6, and 5.

Homeworks and suggested readings



DIP, Sections 3.1, 3.2

- ▶ pp. 105–119



GIMP

- ▶ Colors
 - ▶ Brightness-Contrast
 - ▶ Threshold
 - ▶ Levels
 - ▶ Curves
 - ▶ Invert
 - ▶ Auto
 - ▶ Stretch Contrast
 - ▶ Normalize